

MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANDARDS-1963-A



NAVAL POSTGRADUATE SCHOOL Monterey, California



DTIC ELECTE SEP 2 8 1983

THESIS

POWERPLANT SELECTION FOR CONCEPTUAL HELICOPTER DESIGN

bу

Timothy Joseph Casey

June 1983

Thesis Advisor:

Donald M. Layton

Approved for public release; distribution unlimited.

SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

UPI AUI RAPOMPUIVI	ION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
. REPORY NUMBER		3. RECIPIENT'S CATALOG NUMBER
	41-4/3:29	J.
. TITLE (and Subtitle)		5. TYPE OF REPORT & PERIOD COVERED
Powerplant Selection for		Master's Thesis
Conceptual Helicopter Des	sign	June 1983
		6. PERFORMING ORG. REPORT NUMBER
AUTHORY		S. CONTRACT OR GRANT NUMBER(s)
Timothy Joseph Casey		
PERFORMING ORGANIZATION NAME AND ADD	RESS	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
Naval Postgraduate School	l	
Monterey, California 939	940	
. CONTROLLING OFFICE NAME AND ADDRESS		12. REPORT DATE June 1983
Naval Postgraduate School	1	
Monterey, California 93		13. NUMBER OF PAGES
MONITORING AGENCY NAME & ADDRESS(II di		15. SECURITY CLASS. (of this report)
		Unclassified
		15a. DECLASSIFICATION/ DOWNGRADING SCHEDULE
. DISTRIBUTION STATEMENT (of this Report)		
	ase: distributio	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
Approved for public rele	ase; distributio	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
	ase; distributio	15a. DECLASSIFICATION/ DOWNGRADING SCHEDULE
Approved for public rele		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public rele		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public rele		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public rele		154. DECLASSIFICATION/DOWNGRADING SCHEDULE n unlimited.
Approved for public rele		154. DECLASSIFICATION/DOWNGRADING SCHEDULE n unlimited.
Approved for public release. OISTRIBUTION STATEMENT (of the abotract on		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public release. OISTRIBUTION STATEMENT (of the abotract on		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public release. OISTRIBUTION STATEMENT (of the abotract on		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public release. OISTRIBUTION STATEMENT (of the abotract on		154. DECLASSIFICATION/DOWNGRADING SCHEOULE n unlimited.
Approved for public release. DISTRIBUTION STATEMENT (of the abetract on Supplementary Notes	torod in . Sock 20, If different fro	15a. DECLASSIFICATION/DOWNGRADING n unlimited.
Approved for public release. DISTRIBUTION STATEMENT (of the abetract on Supplementary notes REY WORDS (Continue on reverse side if necessor Engine We	tered in . Seek 20, If different fre	15a. DECLASSIFICATION/DOWNGRADING n unlimited.
Approved for public release. O DISTRIBUTION STATEMENT (of the abetract on Supplementary notes Exer words (Continue on reverse side if necesse Engine We Turboshaft engine Engine	cored in Gook 20, if different from the core and identify by block number, ight estimation gine installatio	n unlimited. n Report) n considerations
Approved for public release. OBTRIBUTION STATEMENT (of the abotract on Supplementary Notes KEY WORDS (Continue on reverse side if necesse Engine We Turboshaft engine Engowerplant selection Rai	ery and identify by block number, ight estimation gine installation age and endurance	n unlimited. n Report) n considerations e for helicopter flight
Approved for public release. OBSTRIBUTION STATEMENT (of the abotract on Supplementary Notes KEY WORDS (Continue on reverse side if necessarine We Turboshaft engine Engowerplant selection Rai	ery and identify by block number, ight estimation gine installation age and endurance	n unlimited. n Report) n considerations

A method of optimizing the selection of a powerplant based upon engine and fuel weight is developed for use in a conceptual helicopter design course. Historical data is analyzed to verify and modify existing formulae used to estimate engine performance and engine installation weight. Computational programs for use on a hand-held computer and the IBM 3033 are developed to predict analytically engine fuel flow characteristics and to optimize engine selection

DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE

Approved for public release; distribution unlimited.

Powerplant Selection for Conceptual Helicopter Design

by

Timothy Joseph Casey
Captain, United States Army
B.S., United States Military Academy, 1973

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN AERONAUTICAL ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL June 1983

Author:

Approved by:

Chairman, Department of Aeronautics

Deag of Science and Engineering

ABSTRACT

A method of optimizing the selection of a powerplant based upon engine and fuel weight is developed for use in a conceptual helicopter design course. Historical data is analyzed to verify and modify existing formulae used to estimate engine performance and engine installation weight. Computational programs for use on a hand-held computer and the IBM 3033 are developed to predict analytically engine fuel flow characteristics and to optimize engine selection.

TABLE OF CONTENTS

I.	INT	RODUCTIO	N		•		•	•	•	•	•	•	•	•	•	•	•	•	6
	A.	BACKGRO	UND .		•		•	•	•	•	•	•	•	•	•	•	•	•	6
	в.	OBJECTI	VES .		•			•	•	•	•	•	•	•	•	•	•		7
II.	APPE	ROACH TO	THE	PROF	BLEM	١.	•	•	•	•	•		•	•	•	•	•		ç
	Α.	OVERVIE	w		•		•	•	•	•	•	•	•	•	•	•	•	•	ç
	В.	BROAD E	VALUA	TION	I CF	RITE	RI.	A	•	•	•	•		•	•	•	•		10
	c.	THE ESS	ENTIA	L CF	RITE	ERIA		PEI	RFC	RM	IAN	CE	2	•	•	•	•	•	11
	D.	PERFORM	ANCE	PARA	MET	ERS		•		•	•	•		•	•	•	•	•	11
	E.	EXTERNA	L FAC	TORS	S AF	FEC	TI	NG	EN	ΙGΙ	NE	2							
		PERFORM	ANCE		•		•	•	•	•	•	•	•	•	•	•	•	•	12
	F.	EXTRACT	ING D	ATA	AND) PR	ED	IC:	ΓIN	īG	PE	RF	OF	RMA	NC	E	•	•	13
	G.	ESSENTI	AL DA	TA.	•		•	•	•	•	•	•	•	•		•	•	•	15
	н.	WEIGHT			•		•	•	•	•	•	•	•	•	•	•	•	•	17
	I.	SELECTI	ON AN	D OF	TIM	IIZA	TI	ON	•	•	•	•	•	•	•	•	•	•	20
III.	SOLU	JTION .			•		•	•	•	•	•	•	•	•	•	•	•	•	23
IV.	RESU	JLTS .			•		•	•	•	•	•	•	•	•	•	•	•	•	25
	Α.	COMPUTA	TIONA	L PF	ROGE	AMS	A	ND	DA	ΥA	1		•	•	•	•	•	•	25
	в.	ACCURAC	Y		•		•	•	•	•	•	•	•	•	•	•	•	•	26
	c.	LIMITAT	IONS		•		•	•	•	•	•		•	•	•	•	•	•	27
	D.	HP-41C	MEMOR	Y RE	QUI	REM	EN'	TS	•	•	•	•	•	•	•	•	•	•	27
v.	CONC	CLUSIONS	AND	RECO	MME	NDA	TI	ONS	3	•	•	•	•	•	•	•	•		28
	A.	USEFULN	ESS F	OR F	REL	IMI	NA:	RY	DE	SI	GN	ſ	•	•	•	•	•		28
	B.	RECOMME	NDATI	ONS	_		_										_		28

LIST OF REFERENCES	. 2	29
APPENDIX A: DEFINITIONS	. 3	31
APPENDIX B: ENGINE SELECTION DATA	. 3	34
A. AVAILABLE POWER PLANTS	. 3	34
B. ENGINE PERFORMANCE AT OTHER THAN STANDARD SE	A	
LEVEL CONDITIONS	. 3	35
C. ENGINE INSTALLED WEIGHT	. 3	35
APPENDIX C: FUEL FLOW AND WEIGHT COMPUTATION USING TH	Œ	
HP-41C	. 3	36
APPENDIX D: FORTRAN ENGINE OPTIMIZER	. 5	58
A. PURPOSE	. 5	5 9
B. INPUT REQUIRED	. 5	5 9
C. OUTPUT	. 6	30
D. EXAMPLE PROBLEM AND USER INSTRUCTIONS	. 6	30
E. ALGORITHM	. 6	32
F. PROGRAM RESULTS	. 6	6
G. COMPUTER PROGRAM	. 6	8
APPENDIX E: HELICOPTER POWER CALCULATIONS FOR THE		
HP-41C	. 8	8€
APPENDIX F: EVALUATION OF ANALYTICAL SOLUTIONS	. 12	0
INITIAL DISTRIBUTION LIST	. 12	:6

I. INTRODUCTION

A. BACKGROUND

The selection of a powerplant in the design process of a helicopter has become an extremely complex task. Mission profile performance, weight, life cycle costs, maintainability, and noise have all become important considerations. Early helicopter designers were concerned only about weight and power available. In fact, until 1876 when N. A. Otto invented the four stroke internal combustion engine, there were no engines with power to weight ratios high enough to enable practical powered flight. It was not until 1907 that a 24 horsepower Antoinette engine provided the power for the first free flight in a helicopter.

Internal combustion engine technology remained well ahead of stability and control design in helicopters through the first half of the 20th century. But in 1954, the H-39 was built by Sikorsky as a test bed for the gas turbine engine (a Turbomeca Artouse II engine), and in 1956 the first version of the UH-1 was flown powered by an American built Lycoming T53-L-11 gas turbine. This design was a major breakthrough in aircraft engines because it significantly reduced the weight while increasing payload and speed over similar utility helicopters driven by reciprocating engines (despite a somewhat lower specific fuel consumption

rate). Continued advancements in turboshaft engine technology over the past 25 years have resulted in a proliferation of engines available for consideration by the
helicopter designer—to the extent that even for preliminary
design some specific guidance is needed toward making a
suitable selection.

The purpose of this study is to develop a process for selecting a powerplant which would best meet preliminary design specifications for a helicopter [Ref. 1]. This process has to be straight-forward enough to be used in an initial design course by graduate students who are not helicopter experts. From an engineering standpoint, initial design of a helicopter to meet given mission and physical specifications focuses upon performance, fuel economy, and weight as primary selection criteria. Those criteria are, therefore, emphasized here.

B. OBJECTIVES

のないない。

In order to accomplish the overall goal of providing a basic guide for the selection of a powerplant in the preliminary design of a helicopter, the following objectives were to be attained:

- 1. Presentation of an outline of powerplant selection criteria with references for more detailed explanation of those major considerations which would not be dealt with in this study.
- 2. A "paring down" of selection criteria to those applicable to an engineering preliminary design course.

- 3. Collection and tabular presentation of accurate data on 6 turboshaft engines which represent current technology performance.
- 4. Development of programs to optimize engine selection using either a hand-held calculator (HP-41C) or the IBM 3033 computer (FORTRAN).
- 5. Verification of data and calculations by comparison with flight manual information for an operational helicopter.

II. APPROACH TO THE PROBLEM

A. OVERVIEW

The selection of a powerplant for a modern helicopter has become so complex that in recent military helicopter programs competing manufacturers designed their aircraft around a particular engine (UH-60A, AH-64, and Lamps III all using versions of the GE T700 engine). In general, research and development costs and time usually limit airframe designers to consideration of existing engines. This approach seemed most realistic and was used in this study (as opposed to developing a "rubber" engine which could have been optimized for use under the design specifications of the particular aircraft being built). The following approach was taken to develop a viable method of evaluating and then selecting the most suitable powerplant available during preliminary design:

- 1. Broad selection criteria were established.
- 2. Performance was reasoned to be the essential criteria for initial design.
- 3. Performance parameters were established.
- 4. External factors affecting engine performance were evaluated.
- 5. Methods of obtaining and extracting engine data were explored.
- 6. Data essential for performance evaluation was determined.

- 7. Weight calculations were researched.
- 8. A selection and optimization process was developed.

B. BROAD EVALUATION CRITERIA

- [Ref. 2] describes four criteria by which to rate the overall mission effectiveness of any major component in military helicopter design. These criteria include three considerations which are operational in nature and a fourth which is economic. They are:
 - 1. Mission Readiness. This includes:
 - a) Mission Capability (specifically, can the component do what it was designed to do).
 - b) Availability (which is a function of reliability and maintainability).
 - 2. Survivability
 - 3. Performance. This is based upon predetermined mission profiles which result in specifications (e.g. hover out of ground effect at maximum gross weight at 4000 feet pressure altitude and 95 degrees ambient temperature).
 - 4. Cost Factors
 - a) Life Cycle Costs
 - i) Research and development.
 - ii) Initial investment.
 - iii) Operational costs (e.g. fuel, personnel and training).
 - iv) Maintenance.

or:

b) Incremental Costs. Only those costs which differ between competing components.

Each of the above factors must be weighed according to its importance to the procuring agency.

C. THE ESSENTIAL CRITERIA--PERFORMANCE

It was realized, after some thought, that the single most important factor in the selection of an existing engine is mission capability. Without this factor, the others have little meaning. The engine must first be able to provide sufficient power to enable the aircraft to do its designed mission. Mission capability is predominantly a function of performance characteristics. For the purposes of preliminary engineering design, then, it seemed most logical and useful to focus upon capability, and thus performance, as the criteria for powerplant selection.

D. PERFORMANCE PARAMETERS

COURT BENEAUCH TO COURT TO COURT TO COURT TO COURT

Performance of a turboshaft engine designed for use in rotary wing aircraft has been traditionally measured in the following ways:

- 1. Output shaft horsepower.
- 2. Specific fuel consumption.
- Power to weight ratio.

These parameters are used in this study as the essential criteria upon which the final selection of an engine is made for use in preliminary design.

E. EXTERNAL FACTORS AFFECTING ENGINE PERFORMANCE

It was found that engine specification manuals prepared by engine manufacturers contained a myriad of technical specifications and performance data. These manuals quite naturally presented the performance characteristics of their engines in the best possible forms. However, numerous qualifications (e.g. altitude, temperature, bleed air, distortion) were placed on the specifications. Extreme care had to be taken in interpreting the data.

[Ref. 3] outlines an array of considerations which should be accounted for before evaluating raw engine performance data extracted from specification manuals. Included are the following:

1. Basic airframe design (as it applies to installation and removal of the engine and to the location of the output shaft).

A POST RESIDENCE DE L'ANNE DE L'ANNE

- 2. Air induction system (perhaps most importantly the particle separator).
- 3. The starting system.
- 4. The lubrication system.
- 5. The cooling system.
- 6. The exhaust system.
- 7. The fuel system.
- 8. The fire protection system.
- 9. Accessories (such as anti-ice and environmental control).

One primary reason for consideration of the above areas is to ascertain the power losses associated with their operation which may not have been accounted for in the engine specifications.

During the preliminary design phase, the details about the systems noted above may not be known and are very probably determined by the final engine selection. Therefore, for the purposes of preliminary design, a conservative estimate of 1-2 percent bleed air and inlet losses were made [Ref. 4]. A reduction by 10 hp. of the published usable shaft horsepower from the engine manuals is included in the analytical solutions used in this study to account for such losses.

Standard practice in the preliminary design of military helicopters requires that fuel flow rates based upon engine specifications be increased by 5 percent in all calculations [Ref. 5]. This conservative procedure allows for handling characteristics and system degradation over time. This 5 percent increase is incorporated in the programs developed in this study.

F. EXTRACTING DATA AND PREDICTING PERFORMANCE

With the above initial considerations made, the next step was extracting relevent performance data from the manufacturer's manuals. Two things were immediately noted:

- Technical performance terminology was difficult to understand but was critical to accurate interpretation of the data. Some particularly important definitions were compiled and are in Appendix A.
- 2. Performance data at standard sea level conditions was always given whereas data at a particular design condition may not have been tabulated.

Since determination of performance characteristics at design specifications is critical, research was conducted on methods by which nonstandard performance data could be obtained. At least three ways of obtaining performance data at specific operating conditions were found:

- 1. Computer programs developed by the manufacturer: (e.g. [Ref. 6] for the T700-GE-401 engine).
- 2. Interpolation of charts sometimes included in the manufacturer's specification manual ([Ref. 7] for the T53 Lycoming series engines).
- 3. Flight data charts from operators manual if the engine was already being used in an operational aircraft ([Ref. 8] for the T400 Pratt Whitney engine).

Computer programs were found to be consistently available on the engines developed within the last 10 years. However these programs were not easily obtained, were complex to use, and often did not interface with available hardware. As a result, each of the above listed methods was used for at least one of the six engines in Appendix B to verify the performance approximations used in this study.

Another method found of predicting engine performance is to digitize published data, then utilize a regression program which results in a formula which predicts engine performance at any desired airspeed or density altitude. Such an approach was taken in [Ref. 9]. This method was found to be very time consuming and was much less accurate than those mentioned above.

G. ESSENTIAL DATA

Minimum essential data for engine performance evaluation was determined to be the following:

•

- 1. Output shaft horsepower available and specific fuel consumption at three power settings at sea level standard conditions. This data provided a basic idea of the power available from the engine as well as sufficient information to calculate fuel flow rate at other pressure altitudes and temperatures (using known shaft horsepower required).
- 2. Maximum static power available at the design conditions and at 25,000 feet. This data allowed engine power evaluation at design (e.g. 4000 ft. and 95 degrees) and hover ceiling specifications (normally below 25,000 ft.).
- 3. Alternately, since the data in 2. above is not consistently available, an approximation of engine power available at nonstandard conditions may be made ([Ref. 10]) using the formula:

$$SHP = \left[\delta/\sqrt{\theta}\right](SHP) \tag{2.1}$$

A comparison of the performance predicted by this formula versus actual data for a sample engine is made in Table I.

It can be seen that this approximation becomes quite conservative at altitudes near normal hover ceilings. However, the results are very reasonable at the design conditions.

Raw engine data may also be correlated with total rotor power required (RSHP) calculations using the following formula [Ref. 1]:

ESHP =
$$1.03 \cdot RSHP + .1 \cdot (n-1) \cdot RSHP + 10$$
 (2.2)

Where n is the number of engines used.

TABLE I
Analytical vs. Actual Engine Performance

20000 ft.	<u>-12 F</u>		
Engine	SHP <u>Actual</u>	SHP Analytical	% Difference
A	214	208	3
В	369	350	5
С	914	772	15
D	1000	891	11
E	1378	1237	10
F	2070	1682	19
4000 ft.	<u>95 F</u>		
Engine	SHP Actual	SHP <u>Analytical</u>	% Difference
A	325	356	9
В	583	601	3
С	1170	1325	13
D	1404	1529	9
E	2055	2123	3
F	3086	2888	6

Engines

A: T63-A720 D: T400-CP-400 B: LTS101-750A E: T55-L-7 C: T700-GE700 F: T55-L-712

H. WEIGHT

Engine dry weight is normally provided with performance data. However, an installed weight of the engine offers much more accurate weight estimation for power calculations. The installed weight is defined here to include:

- a. Lubricant weight.
- b. Cooling system.
- c. Engine controls.
- d. Engine supports.
- e. Exhaust ducting.
- f. Starting system.

Methods to accurately estimate an engine's installed weight were investigated. Analysis of data collected on current helicopter installed weights revealed that the "rule of thumb" formulae in use in [Ref. 1] correctly predict weight trends. However, the installed weights calculated using those formulae are somewhat low for engine dry weights up to about 700 pounds. Since this range of engines includes approximately 70 percent ([Ref. 11]) of the helicopters in production in the West, an attempt to update the weight estimating relationship is made here.

A search of the literature revealed at least two additional methods of engine weight estimation:

1. Powerplant weight estimation based upon maximum horsepower of the engine [Ref. 12] using the following equation:

$$W_{EI} = 130.243 + .369$$
Hp

2. Installation weight as a function of engine dry weight [Ref. 13]; with the percentage of installation weight increasing with engine dry weight according to the formula:

$$W_{EI} = .0974(W_{ED})^{1.2}$$

It was found that method 1 was based upon data taken from early model helicopters which does not reflect current technology. Additionally, the components included in the total installed engine weight were inconsistent between different aircraft manufacturers. This problem arose in the collection of data for this study as well. As an example, Bell Helicopter Textron (BHT) includes only residual fuel and oil in the published values of installed engine weight. Individual component installation weight and balance information had to be obtained from Bell to get data which would be consistent for comparison and analysis.

Method 2 above does not coincide with the design trends reflected by the U.S. helicopters analyzed in this study.

In order to determine an accurate method of estimating engine installed weight, a data base of 20 helicopters was collected. Table II depicts the aircraft, engines, engine weights and engine horsepowers used for the data base. The helicopters in this table include many of the U.S. military rotary wing aircraft currently operational [Ref. 14], [Ref. 15], [Ref. 16].

TABLE II Turboshaft Engine Data Base

Engine	A/C	Dry Weight lbs	Installe	
T63-A-5A	ОН-6А	136.0	175.2	317
A11-250-C18	Th-57A	136.0	194.0	317
T63-A-720	OH-58C	158.0	218.0	420
T58-GE-8F	UH-2D	305.0	403.0	1350
T58-GE-5	S-67	335.0	471.0	1500
T58-GE-10	CH-47D	340.0	454.0	1400
T700-GE-700	ҮАН-63	423.0	547.0	1560
T700-GE-701	AH-64	427.0	587.0	1690
T58-GE-16	CH-46E	430.0	621.0	1870
T53-L-703	AH-1S	495.0	607.0	1485
T53-L13	UH-1H	540.0	683.0	1400
T55-L-7	CH-47A	580.0	671.0	2650
T64-GE-16	AH-56	700.0	969.0	3370
T400-CP400	UH-1N	701.0	910.0	1800
T400-CP400	AH-1J	701.0	908.0	1800
T64-GE-6	CH-53A	723.0	881.0	2850
T400-WV-402	AH-1T	733.0	936.0	1970
T55-L-11D	CH-47C	735.0	897.0	3750
T55-L712	CH-47D	760.0	925.0	3400
JTFD12A-4A	CH-54A	920.0	1093.0	4500
Several curve	fitting	techniques	were applied	to engine
modelhe ondeon	ia baaad	+ h = 0.0	conomoto com	aniconc.

- 1. Engine dry weight vs. installation weight as a percentage of dry weight.
- 2. Engine military horsepower available vs. total installed weight.
- 3. Engine dry weight vs. total installed weight.

 It was found that the best weight estimating relationship could be obtained using comparison 3 with a linear regression. The weight estimating relation is:

$$W_{EI} - 44.684 + 1.193W_{ED}$$

For consistency with other equations used for helicopter preliminary design, this formula is rounded to two significant figures:

$$W_{EI} = 45 + 1.2W_{ED}$$
 (2.3)

This relationship yielded an R² value of .9819. Figure 1 is a plot of installed weight estimation based on equation 2.3.

I. SELECTION AND OPTIMIZATION

The engines at Appendix B are considered as those which are available for the purposes of preliminary design selection here. Those engines were selected for inclusion in this study for the following reasons:

- 1. Currently in use in military helicopters with accurate and tested data available.
- 2. Representative spectrum of shaft horsepower required in military rotorcraft.
- 3. Latest developments incorporated (SFC and weight especially).
- 4. Variety of manufacturers [Ref. 7], [Ref. 17], [Ref. 18], and [Ref. 19].

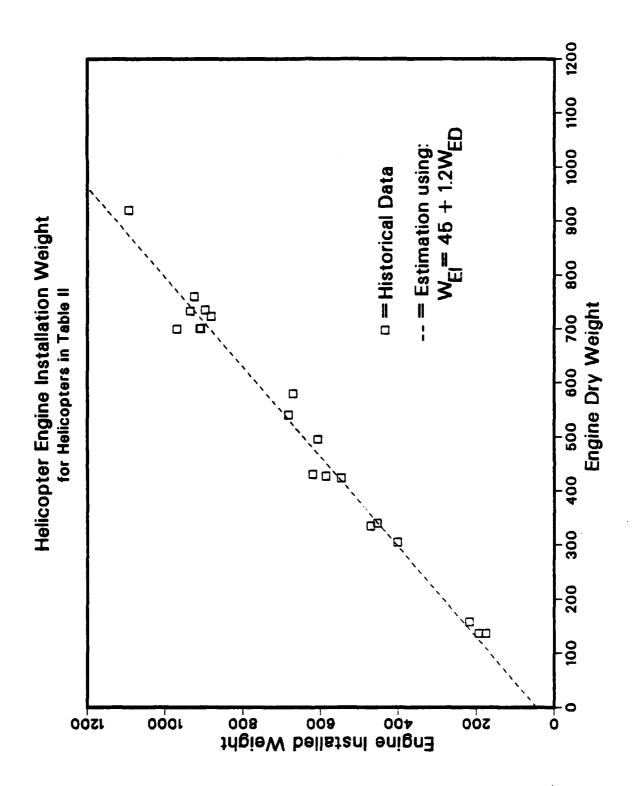


Figure 2.1 Engine Dry Weight vs. Installed Weight

Essentially, an engine(s) which would fulfill a specific mission capability could have been selected by inspection almost at random from this list once power requirements were determined. However, it seemed much more realistic to optimize the selection in some way.

The most useful method of selecting the "best" engine(s) in a preliminary design process appears to be one in which the minimum total weight is obtained (enabling the biggest payload, most range, or most additional equipment installed). The total weight includes the total fuel weight required by the engine to accomplish a specified mission as well as the installed weight of the powerplant itself. The estimation of engine installed weight is made using equation 2.3. The total fuel required is calculated using the mission criteria stated in [Ref. 1]:

Fuel Wt. =
$$.05W_f$$
 < NRP> + W_f < cruise>*Range < max>/V < cruise> + $.25W_f$ < V < end>> + $.05W_f$ < NRP> (2.4)

The optimum powerplant is then determined by adding the fuel and engine(s) weights and using the smallest value found.

III. SOLUTION

The calculations necessary to make the total weight comparisons were initially done manually using equations and the mission profile from [Ref. 1]. Then programs were developed to aid in the optimization process. Considerations in the development of the computer programs are:

TO A PROGRESSION AND TRANSPORTED TO A SECOND SECOND

- 1. Compatibility with previous work using both a handheld calculator and a main frame computer.
- 2. Reasonable simplicity so that the feel for the design process is not lost within the computing machine.
- 3. Flexibility and adaptability (easily modified or expanded).
- 4. Output of intermediate data required for helicopter design (e.g. fuel flow rates) as well as final comparisons.
- 5. Weight used as the optimization criteria.

Three basic computer programs were written, two for use on the HP-41C and the third for interactive use on the IBM 3033. All programs assume that calculations for rotor shaft horsepower required (RSHP) can be made. Inputs required are:

- 1. Engine SHP and SFC at three power settings at sea level standard day conditions.
- 2. Pressure altitude and temperature.
- 3. Dry weight of engine.

4. Access to power equations: "Flite" [Ref. 20], "Power" (Appendix E), or the Helicopter Computation Package [Ref. 21].

Program outputs are:

- 1. Zero shaft horsepower intercept.
- 2. Slope of fuel flow vs. ESHP line.
- 3. Phantom SHP [Ref. 22].
- 4. Fuel flow rate at desired RSHP and density altitude.
- 5. Total fuel weight for mission profile.
- 6. Total weight of fuel plus installed powerplant.
- 7. Recommended selection between two candidate power-plants (FORTRAN program only).

IV. RESULTS

A. COMPUTATIONAL PROGRAMS AND DATA

The research and programming results of this study are presented in Appendices C thru E:

- 1. Appendix C contains the fuel flow characteristics and the engine and mission fuel weight calculation programs for the hand-held calculator. The fuel and engine weight program requires the user to manually compare total weights calculated for each engine analyzed. This procedure was followed to save calculator register space. Also in Appendix C are program flow charts and sample problems.
- 2. Appendix D contains the FORTRAN engine optimizer as well as the program algorithm and a sample problem.
- 3. Appendix E contains three supporting programs for use with the HP-41C calculator:
 - a. "Power" which calculates the total power required for a helicopter in level flight. This program was developed to enable rapid calculation of fuel flow characteristics at varying conditions and design parameters. It was found that total power calculations using existing programs for the HP-41C were very cumbersome to use for the purpose of determining fuel flow and fuel weight data.
 - b. "VE" which computes the maximum endurance velocity for the preliminary design of a helicopter. This program uses "POWER" iteratively to achieve a solution for maximum endurance velocity.
 - c. "VMR" which computes the maximum range velocity for the preliminary design of a helicopter. This program uses "POWER" iteratively to achieve a solution for maximum range velocity.

B. ACCURACY

Appendix F contains a comparison between actual performance for the UH-60A (Blackhawk) helicopter [Ref. 23], and the analytical results obtained by the use of the computational programs in Appendices C thru E. Tables XI-XIII show that the analytical results obtained agree quite well with actual helicopter performance. Although only one helicopter was used to evaluate the program outputs, an encouraging indication of their accuracy is at least provided. However, it can be seen that at higher airspeeds (especially at nonstandard conditions) the analytical solutions become increasingly less exact. This is primarily a function of the basic nature of the equations used to predict rotor power required for a preliminary helicopter design. Several real world conditions are not modeled by the equations (... g. rotor downwash on the fuselage, compressibility effects, and blade stall). Such conditions result in higher actual power requirements than those predicted (especially above about 120 knots).

The basic equations used to predict fuel flow rates, however, appear to model actual conditions extremely well. Table XI shows consistently lower error for fuel flow rate analytical results than for predicted engine shaft horsepower required. Additionally, when the actual engine shaft horsepower required from the operator's manual was used to

calculate fuel flow rate, the result was within 5 percent of chart values in every case compared.

C. LIMITATIONS

- 1. Modeling of required rotor power does not include all aerodynamic effects. These limitations are discussed in [Ref. 24].
- 2. Accuracy at non-standard conditions and airspeeds greater than 120 knots is only fair; nonlinearities of the fuel flow lines are not considered.
- 3. Maximum and minimum engine fuel flow rates are not considered.
- 4. Changes in engine shaft horsepower available with temperature and altitude are not programmed. These changes must be checked manually (see Appendix B).

D. HP-41C MEMORY REQUIREMENTS

The programs listed in Table III use a total of 239 registers of program memory. Size 46 is required to provide sufficient memory storage for all programs.

TABLE III
PROGRAM STORAGE REGISTER REQUIREMENTS

Subject Area		gram Registers	Subroutine Name Register:				
Engine fuel flow characteristics	FUELFL	56					
Mission fuel and engine weights	WEIGHT	30	FUELFL	56			
Total helicopter power required	POWER	106					
Maximum endurance velocity	VE	22	POWER	106			
Maximum range velocity	VMR	25	POWER	106			

V. CONCLUSIONS AND RECOMMENDATIONS

A. USEFULNESS FOR PRELIMINARY DESIGN

The programs developed in this study and the equations used in their development appear to provide an excellent basis upon which to conduct the preliminary design of a modern helicopter. The use of the programs requires a reasonable understanding of helicopter performance and the user should carefully execute the example problems to insure understanding of the computational process. Since all of the programs developed here build upon existing code, complexity has increased; hopefully however, not at the expense of clarity.

B. RECOMMENDATIONS

- 1. Comparisons of analytical results with actual performance data for a number of operational helicopters should be conducted. The true applicability of the equations and programs used here can best be determined in this way.
- 2. UH-60A operational data indicate that analytically predicted power requirements and fuel flow rates could be brought to within 5-10 percent accuracy simply by increasing the loss factor between the engine and the rotor by 15 percent. That is by letting:

$$ESHP = ((.1*N) + 1.18)*RSHP + 10$$

Such an increase may better account for power reductions resulting from pressure losses and accessories. The validity of changing the loss factor in this manner needs to be verified by making the additional comparisons recommended in 1 above.

LIST OF REFERENCES

- 1. Kee, Stephen G., <u>Guide for Conceptual Helicopter Design</u>, M.S. Thesis, Naval Postgraduate School, 1983.
- 2. Engineering Design Handbook, <u>Helicopter Engineering</u>
 Preliminary Design, Part I, AMCP 706-201, U.S. Army
 Material Command, August 1974.
- 3. Ibid., pp. 3-25.

- 4. Ibid., pp. 8-12.
- 5. Ibid., pp. 3-110.
- 6. Ferguson, J. A., The User's Manual for Computer Program
 T700/78010 for the T700-GE-401 Engine, Term Paper for
 AE 4900, Naval Postgraduate School, 1982.
- 7. AVCO Lycoming Division Model Specification No. 104.33, T53-L13 /A/B/ Shaft Turbine Engines, 30 September 1969.
- 8. NATOPS Flight Manual, NAVAIR 01-11-HCB-1, Navy Model AH1-J Aircraft, 1 February 1979.
- 9. O'Neil, G. S., <u>Helo Design Engine Performance Estimates</u>, Term Paper for <u>AE 4900</u>, Naval Postgraduate School, 1981.
- 10. Layton, Donald M., Aircraft Performance, p. 51, Naval Postgraduate School, 1982.
- 11. "Aerospace Outlook: Specifications," Aviation Week and Space Technology, v. 116, pp. 148-154, 8 March 1982.
- 12. National Aeronautics and Space Administration Report CR 152315, Parametric Study of Helicopter Systems

 Costs and Weights, by M. N. Beltramo and M. A. Morris, pp. 4-23-4-28, January 1980.
- Applied to Advanced Rotary Wing Concepts, Scholarly Paper submitted for M.S., Aerospace Engineer, University of Maryland, May 1978.
- 14. Boeing Vertol Division, Letter to the Naval Postgraduate School, Subject: <u>Installed Engine Weights</u>, 28 February 1983.

- 15. Hughes Helicopter Inc., Letter to the Naval Postgraduate School, Subject: <u>Installed Engine Weights</u>, 7 February 1983.
- 16. Bell Helicopter Textron, Letter to the Naval Postgraduate School, Subject: <u>Installed Engine Weights</u>, 3 February 1983.
- 17. AVCO Lycoming Division Model Specification No. 124.53(A), T55-L-712 Turboshaft Engine, 15 January 1981.
- 18. AVCO Lycoming Division Model Specification No. 101.14.30, LTS 101-750A-1 Turboshaft Engine, November 1981.
- 19. The General Electric Company, Contract: DARCOM-CP-2222-02000B, T700-GE700 Turboshaft Engine, pp. 92-93, 8 April 1981.
- 20. Layton, Donald M., <u>Helicopter Performance Programs for the HP-41</u>, Naval Postgraduate School, 1983.
- 21. Sullivan, Patrick, <u>Helicopter Power Computation Package</u>, Term Paper for AE 4900, Naval Postgraduate School, 1982.
- 22. Layton, Donald M., <u>Helicopter Performance</u>, Naval Post-graduate School, 1980.
- 23. Department of the Army Technical Manual TM 55-1520-237-10, Operator's Manual UH-60A Helicopter, pp. 7-1--7-50, 21 May 1979.
- 24. Fardink, Paul J., <u>Hand-Held Programs for Preliminary</u>
 <u>Helicopter Design</u>, M.S. Thesis, Naval Postgraduate
 <u>School</u>, 1982.

STATES AND STATES AND STATES

APPENDIX A

DEFINITIONS

Absolute Altitude: The maximum altitude at which the engine will function properly under specified ram pressure ratios.

Cold Atmospheric Conditions: Cold atmospheric air pressures are given in MIL-STD-210. Cold atmospheric air temperature is -54.3 C from sea level to 25,500 feet altitude.

<u>Cruise Power</u>: Most often defined as 75 percent of normal rated power, but may be a different percentage, especially in older engine manuals.

ESHP: Used in this study to specifically designate Engine Shaft Horsepower. However, this term is also defined as Equivalent Shaft Horsepower by engine manufacturers. Equivalent Shaft Horsepower is a modified power output rating which includes jet thrust:

Static ESHP = SHP + $F_n/2.5$

Flight ESHP = SHP + $(F_n \times V)/261$

where: F_n is net jet thrust in pounds.

V is flight speed in knots.

Gross Jet Thrust: The thrust delivered at the exhaust duct exit as determined from the product of exhaust gas mass flow and velocity, plus exhaust duct area times the difference between gas static pressure and ambient exhaust pressure.

Hot Atmospheric Conditions: Hot atmospheric air pressures are given in MIL-STD-210. Hot atmospheric temperature is 55 C at sea level and decreases at a rate of .0025 C per foot of altitude to 38,000 feet altitude.

<u>Inlet Air Distortion</u>: Steady state and dynamic inlet air pressure variations and steady state temperature variations as defined by Distortion Indexes (DI) of the form:

$$DI = \frac{(P_{T_{MEAN}} - P_{T_{LOW MEAN}})}{P_{T_{MEAN}}}$$

$$DI = \frac{(T_{1_{MAX}} - T_{1_{MEAN}})}{T_{1_{MEAN}}}$$

Military Rated Power: The highest power at which the engine may be operated for a 30 minute period without special maintenance, provided such operation is followed by a return to Normal Rated Power or lower power for a specified time.

Net Jet Thrust: Gross Jet Thrust minus the product of engine air mass flow and free stream velocity.

Normal Rated Power (NRP): The highest power at which the engine may be operated continuously without restriction (other than scheduled maintenance); also referred to as maximum continuous power.

Ram Efficiency: The ratio of inlet air total pressure to free stream air total pressure.

Shaft Horsepower (SHP): The horsepower delivered at the output shaft of the engine.

Specific Fuel Consumption (SFC): The weight of fuel consumed by the engine in pounds of fuel per hour per shaft horsepower.

APPENDIX B

ENGINE SELECTION DATA

A. AVAILABLE POWER PLANTS

The power plants in Table IV are those considered available for preliminary design selection.

TABLE IV

Available Power Plants

Engine	Dry Weight	Stan	dard Sea	Level Performance
	(<u>lbs</u>)		SHP	SFC
A	158	М:	420	.650
(T63-A-720)		N:	370	.651
,		C:	278	.709
В	268	М:	708	.573
(LTS101-750A)		N:		.573
,,		C:	494	.599
С	423	М:	1561	.460
(T700-GE-700)			1318	.470
(1111 11 11)		C:		.510
D	709	М:	1800	.595
(T400-CP-400)			1530	.606
Note: Dual eng	ine with		1148	.661
single g				
Е	580	М:	2500	.615
(T55-L-7)		N:		.622
• - /		C:		.678
F	750	М:	3400	.543
(T55-L-712)		N:		.562
, , , , , , , , , , , , , , , , , , , ,		C:	2250	.610

M: Military Power N: Normal Power C: Cruise Power

B. ENGINE PERFORMANCE AT OTHER THAN STANDARD SEA LEVEL CONDITIONS

The effects of altitude and temperature on engine performance may be approximated using the formula:

ESHP =
$$(\delta/\sqrt{\theta})$$
 (ESHP)

Where $\delta = P/P_{SSL}$
 $\theta = T/T_{SSL}$ (Absolute temperature)

C. ENGINE INSTALLED WEIGHT

Engine installed weight includes the dry engine(s) weight plus an installation fraction which includes: air induction system, exhaust system, cooling, controls, starting system, mounts, and residual fuel and oil. The total installed weight may be computed as:

$$W_{EI} = 45. + 1.2 \cdot W_{ED}$$
 (per engine)

APPENDIX C

FUEL FLOW AND WEIGHT COMPUTATION USING THE HP-41C

This appendix contains the programs developed for use with the HP-41C programmable calculator. Two main programs were written:

1. FUELFL

- a. Computes fuel flow characteristics from engine standard sea level performance data (SFC and SHP).
- b. Computes fuel flow rate for an input value of rotor shaft horsepower required.

2. WEIGHT

- a. Computes estimated engine installed weight.
- b. Requires prior execution of "FUELFL" to compute fuel flow rates.
- c. Computes total weight of installed engine and fuel for a design mission profile.

Both programs are designed to accept direct user input of required rotor power or to accept a user specified forward velocity and calculate total rotor power required using the program "POWER" in Appendix E. "POWER" was developed to enable rapid calculation of total power required at any forward velocity (or hover) for use in the above programs as well as for calculation of maximum endurance velocity and maximum range velocity (Appendix E).

FUELFL

1. Purpose

This program computes the fuel flow rate for a specific engine for input values of altitude (up to 36,000 feet), temperature and rotor shaft horsepower required. The user must input engine performance data at military, normal, and cruise power settings at sea level from manufacturer's specifications. The program incorporates an increase by 5 percent of specification fuel consumption in accordance with accepted military design criteria.

"FUELFL" is designed with two subroutines which allow calculation of fuel flow rates at varying operating conditions after one initial entry of engine performance data. They are:

- a. "FF" which computes the fuel flow rate for an input value of rotor shaft horsepower required (or velocity if "POWER" is used). This subroutine converts rotor power into engine power by adding power losses in the transmission and drive train as well as power consumed by accessories.
- b. "OPCON" which contains "FF" but which also prompts for current environmental operating conditions.

If "POWER" is to be used to calculate rotor shaft horsepower required, it must be run first so that design data for a specific helicopter may be calculated and stored.

The fuel flow characteristics calculated and displayed are as follows:

Display:

Explanation:

BETA =

Average slope of fuel flow line.

ALPHA =

Zero horsepower intercept per engine at standard sea level

conditions.

ZHI =

Zero horsepower intercept per engine at operating conditions.

PSHP =

Zero velocity horsepower (Phantom

SHP).

WF =

Fuel flow rate (lb/hr).

2. Equations

$$SFC_i = (SFC_i + .05 \times SFC_i)$$
 $i = M, N, C$ (5% increase)

$$W_{f_i} = SFC_i \times SHP_i$$

$$\hat{\beta} = \frac{\mathbf{W}_{\mathbf{f}_{\mathbf{M}}} - \mathbf{W}_{\mathbf{f}_{\mathbf{N}}}}{\mathbf{SHP}_{\mathbf{M}} - \mathbf{SHP}_{\mathbf{N}}} + \frac{\mathbf{W}_{\mathbf{f}_{\mathbf{M}}} - \mathbf{W}_{\mathbf{f}_{\mathbf{C}}}}{\mathbf{SHP}_{\mathbf{M}} - \mathbf{SHP}_{\mathbf{C}}} + \frac{\mathbf{W}_{\mathbf{f}_{\mathbf{N}}} - \mathbf{W}_{\mathbf{f}_{\mathbf{C}}}}{\mathbf{SHP}_{\mathbf{N}} - \mathbf{SHP}_{\mathbf{C}}} \div 3$$

$$\hat{\alpha} = |\hat{\beta}| (SHP_M + SHP_N + SHP_C) - (W_{f_M} + W_{f_N} + W_{f_C})| \div 3$$

$$\delta = P/P_{SSL} = [1 - (h_p \times 6.8754. \times 10^{-6})]^{5.256}$$

$$\sqrt{\theta} = \sqrt{T/T_{SSL}} = \sqrt{\frac{T + 459.688}{518.688}}$$

ZHI = $\hat{\alpha}(\delta\sqrt{\theta})$

$$PSHP = \frac{n(ZHI)}{\hat{\beta}}$$
 AND $ESHP = 1.03(RSHP) + .1(n-1)(RSHP) + 10$

 $W_{r} = [PSHP + ESHP] \hat{\beta}$

where:

SFC is specific fuel consumption (lb/hr/shp)

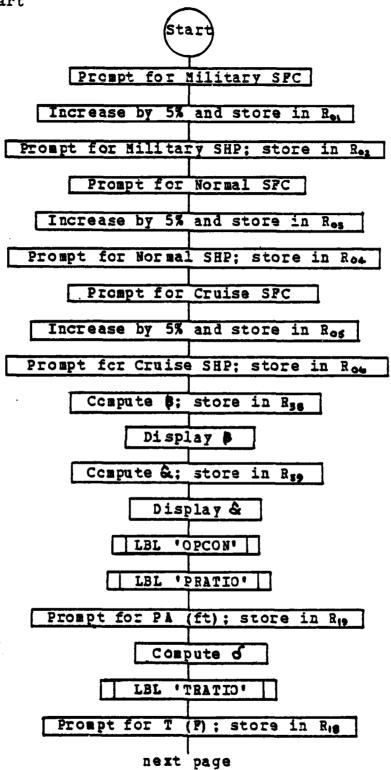
SHP is shaft horsepower of the engine

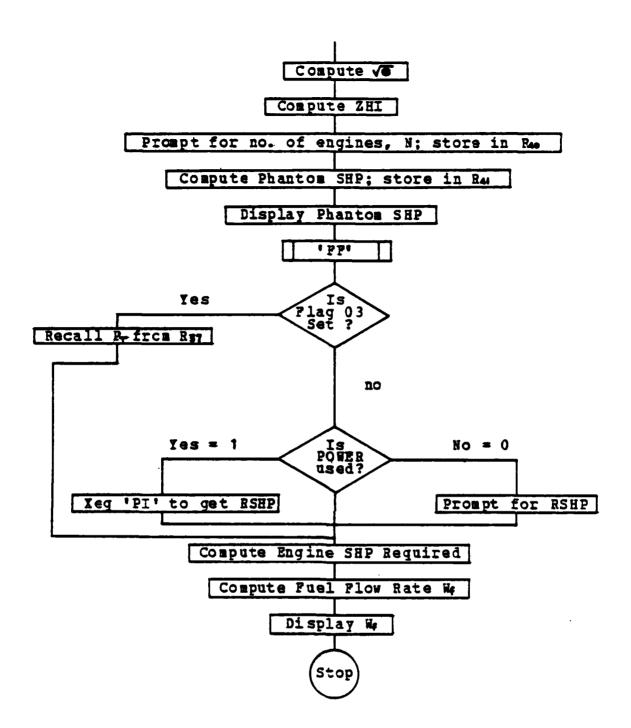
W_f is fuel flow rate (lb/hr)

 $\hat{\beta}$ is the average slope of the fuel flow line

â	is the zero horsepower increment for one engine at standard sea level conditions
δ	is the ratio of pressure to standard sea level pressure
P	is atmospheric pressure at operating conditions (psi)
PSSL	is standard sea level atmospheric pressure (psi)
h _p	is pressure altitude (ft)
θ	is the ratio of temperature to standard sea level temperature (absolute)
T	is temperature in degrees F
ZHI	is the zero horsepower increment at input conditions
n	is the number of engines
PSHP	is the zero velocity horsepower (Phantom SHP)
ESHP	is the engine shaft horsepower required

3. Flowchart





4. Example Problem and User Instructions Find the fuel flow rate for a helicopter under the following conditions:

Engine Data	Operating conditions:
SHP SFC	
Military 1561 .460	Standard Sea Level
Normal 1310 .470	PA = 0
Cruise 989 .510	T = 59 F
Two engines $(N = 2)$	
a. Assume "POWER" will not	be used:
RSHP = 500 hp	
Keystrokes:	Display:
(XEQ) (ALPHA) FUELFL (ALPHA)	SFC-M?
0.460 (R/S)	SHP-M?
1561 (R/S)	SFC-N?
0.470 (R/S)	SHP-N?
1310 (R/S)	SFC-C?
0.510 (R/S)	SHP-C?
989 (R/S)	B = 0.3948
(R/S)	ALPHA = 135.32
(R/S)	PA=?
0 (R/S)	T(F)=?
59 (R/S)	ZHI = 135.32
(R/S)	N=?
2 (R/S)	PSHP = 685.46

POWER?

(R/S)

O(R/S) RSHP=?

500 (R/S) WF = 497.68

Now use "FF" to compute the fuel flow rate for the same engine at the same altitude and temperature but with:

RSHP = 700 shp

Keystrokes: Display:

(XEQ) (ALPHA) FF (ALPHA) POWER?

O(R/S) RSHP=?

700 (R/S) WF = 586.91

Now use "OPCON" to compute the fuel flow rate for the same engine at:

PA = 4000 ft

T = 95 F

RSHP = 700 shp

Keystrokes: Display:

(XEQ) (ALPHA) OPCON (ALPHA) PA. FT.?

4000 (R/S) T <F>?

95 (R/S) ZHI = 120.86

(R/S) N=?

2 (R/S) PSHP = 612.20

(R/S) POWER?

O(R/S) RSHP=?

700 (R/S) WF = 557.99

b. If "POWER" is loaded and executed using the sample helicopter design data included as an example with the "POWER" user instructions, run "FUELFL" again with the same engines and operating conditions but with:

VF = 95 kts

Keystrokes:	Display:
(XEQ) (ALPHA) FUELFL (ALPHA)	SFC-M?
0.460 (R/S)	SHP-M?
1561 (R/S)	SFC-N?
0.470 (R/S)	SHP-N?
1310 (R/S)	SFC-C?
0.510 (R/S)	SHP-C?
989 (R/S)	B = 0.3948
(R/S)	ALPHA = 135.32
(R/S)	PA=?
0 (R/S)	T(F)=?
59 (R/S)	ZHI = 135.32
(R/S)	N=?
2 (R/S)	PSHP = 685.46
(R/S)	POWER?
1 (R/S)	PA=?
0 (R/S)	T <f>=?</f>
59 (R/S)	VF=?
95 (R/S)	PT = 499.17
(R/S)	PT = 499.17
(R/S)	WF = 497.31

Note: When "POWER" is used, the user is prompted for PA and T twice. This is to insure that both engine performance and rotor power required are computed at the same atmospheric conditions.

Now use "FF" to compute the fuel flow rate for the same engine at the same altitude and temperature but with

VF = 120 kts

Keystrokes: Display:

(XEQ) (ALPHA) FF (ALPHA) POWER?

1 (R/S) PA=?

0 (R/S) T<F>=?

59 (R/S) VF=?

120 (R/S) PT = 706.50

(R/S) PT = 706.50

(R/S) WF = 589.82

Now use "OPCON" to compute the fuel flow rate for the same engine at:

PA = 4000 ft

T = 95 F

VF = 120 kts

Keystrokes: Display:

(XEQ) (ALPHA) OPCON (ALPHA) PA. FT.?

4000 (R/S) T<F>?

95 (R/S) ZHI = 120.86

(R/S) N=?

2 (R/S) PSHP = 612.20

(R/S) POWER?

1 (R/S) PA=?

4000 (R/S) T<F>=?

95 (R/S) VF=?

120 (R/S)

PT = 634.12

(R/S)

PT = 634.12

(R/S)

WF = 528.60

5. Programs and Subroutines Used

"FUELFL"

"OPCON"

"PRATIO"

"TRATIO"

"FF"

6. Storage Register Utilization

Table V shows specific storage register contents.

TABLE V
FUELFL Storage Register Utilization

Storage	
Register 00	Stored Quantity blank - used for computations
01	SFC _M - specific fuel consumption at military power at sea level (lb/hr/hp)
02	SHP _M - shaft horsepower output at military power at sea level (hp)
03	SFC _N - specific fuel consumption at normal power at sea level (lb/hr/hp)
04	SHP _N - shaft horsepower output at normal power at sea level (hp)
05	SFC _C - specific fuel consumption at cruise power at sea level (lb/hr/hp)
06	SHP _C - shaft horsepower output at cruise power at sea level (hp)
07	W _f - fuel flow rate at sea level military power with 5% increase (lb/hr)
08	W _f - fuel flow rate at sea level normal N power with 5% increase (lb/hr)
09	W _f - fuel flow rate at sea level cruise power with 5% increase (lb/hr)
10-37	- used by program "POWER"
38	$\hat{\beta}$ - average slope of the fuel flow line
39	$\hat{\alpha}$ - average zero horsepower intercept at standard sea level conditions (lb/hr)
40	n - number of engines in the helicopter
41	PSHP - zero velocity shaft horsepower (phantom shp)

Note: registers 00-09 are also used by other programs.

7. Program Listings

01+LBL "FUELFL"	51	CLX
02 *SFC-M?*	52	RCL 97
03 PROMPT	53	RCL 09
04 STO 01	54	-
95 .95		RCL 92
96 *		RCL 86
97 ST+ 91	57	_
92 -SHP-H?-	58	
89 PROMPT		
- · · · · · · · · · · · · · · · · · · ·		ABS 70
19 STO 92		ST+ 38
11 "SFC-N?"		CLX
12 PROMPT		RCL 98
13 STO 03		RCL 89
14 .05	64	-
15 *	65	RCL 84
16 ST+ 03	66	RCL 96
17 "SHP-N?"	67	-
18 PROMPT	68	
19 STO 94		ABS
20 "SFC-C?"		ST+ 38
21 PROMPT	71	
22 STO 65		ST/ 38
23 .05		RCL 38
24 *		FIX 4
25 ST+ 05	75	-8=-
26 "SHP-C?"	76	ARCL X
27 PROMPT	76 77	ARCL X GVIEW
27 PROMPT 28 STO 06	76 77	ARCL X
27 PROMPT 28 STO 06 29 RCL 01	76 77 78	ARCL X GVIEW
27 PROMPT 28 STO 06	76 77 78 79	ARCL X AVIEW STOP
27 PROMPT 28 STO 06 29 RCL 01	76 77 78 79	ARCL X AVIEW STOP FIX 2 RCL 02
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 *	76 77 78 79 80 81	ARCL X GVIEW STOP FIX 2 RCL 02
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07	76 77 78 79 8 0 81 92	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03	76 77 78 79 80 81 92 83	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04	76 77 78 79 80 81 82 83 84	ARCL X GVIEW STOP FIX 2 RCL 02 * CHS RCL 07 +
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 *	76 77 78 79 80 81 82 83 84	ARCL X GVIEW STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08	76 77 78 79 80 81 82 83 84 85	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05	76 77 78 79 80 81 82 83 84 85 86	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06	76 77 78 79 80 81 82 83 84 85 86 87	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 87 + STO 39 CLX RCL 38 RCL 04
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 *	76 77 78 79 80 81 82 83 84 85 86 87 88	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 *
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09	76 77 78 79 80 81 82 83 84 85 86 87 88 89	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 * CHS
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX	76 77 78 79 80 81 82 83 84 85 86 87 88 89 96	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 * CHS RCL 08
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07	76 77 78 79 80 81 82 83 84 85 86 87 88 89 91	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 08 + CHS RCL 08 +
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08	76 77 78 79 80 81 82 83 84 85 86 87 88 99 91 92	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 * CHS RCL 08 + STH 39
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08	76 77 78 79 80 81 82 83 84 85 86 87 88 99 91 92 93	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 * CHS RCL 08 + ST+ 39 CLX
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08 44 - 45 RCL 02	76 77 78 79 80 81 82 83 84 85 86 87 88 91 92 93	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX RCL 38 RCL 04 * CHS RCL 08 + ST+ 39 CLX RCL 38
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08	76 77 78 79 80 81 82 83 84 85 86 87 88 91 92 93 94	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS 7 + STO 39 CLX 38 RCL 04 * CHS 87 CLX 38 RCL 04 RCL 38 RCL 08
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08 44 - 45 RCL 02	76 77 78 79 80 81 82 83 84 85 86 87 88 91 92 93	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS 7 + STO 39 CLX 38 RCL 04 * CHS 87 CLX 38 RCL 04 RCL 38 RCL 08
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08 44 - 45 RCL 02 46 RCL 04	76 77 78 79 80 81 82 83 84 85 86 87 88 91 92 93 94 95	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS 7 + STO 39 CLX 38 RCL 04 * CHS 87 CLX 38 RCL 04 RCL 38 RCL 08
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08 44 - 45 RCL 02 46 RCL 04 47 - 48 /	76 77 78 79 80 81 82 83 84 85 86 87 88 89 91 92 93 94 95	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX 38 RCL 08 * CHS RCL 08 * CHS RCL 08 * CHS RCL 08 CLX 38 CX 38 C
27 PROMPT 28 STO 06 29 RCL 01 30 RCL 02 31 * 32 STO 07 33 RCL 03 34 RCL 04 35 * 36 STO 08 37 RCL 05 38 RCL 06 39 * 40 STO 09 41 CLX 42 RCL 07 43 RCL 08 44 - 45 RCL 02 46 RCL 04 47 -	76 77 78 79 80 81 82 83 84 85 86 87 88 89 91 92 93 94 95	ARCL X GVIEN STOP FIX 2 RCL 02 * CHS RCL 07 + STO 39 CLX 38 RCL 08 * CHS RCL 08 CHS RCL 08 CHS RCL 08 RCL 08 RCL 08 RCL 08

101 ST+ 39 192 3 193 ST/ 39 104 RCL 39 105 CLA 106 "ALPHA=" 197 ARCL X 108 AVIEW 109 STOP 110+LBL -OPCON-111+LBL -PRATIO-112 "P.A. FT?" 113 PROMPT 114 6.8754 E-6 115 * 116 CHS 117 1 118 + 119 ENTERT 129 5.256 121 YtX 122 STO 92 123+LBL "TRATIO" 124 °T (F)?" 125 PROMPT 126 459.688 127 + 128 518.688 129 / 138 SQRT 131 STO 93 132 RCL 39 133 RCL 92 134 * 135 RCL 93 136 * 137 "ZHI=" 138 ARCL X 139 AVIEW 148 STOP 141 RCL 38 142 / 143 "H=?" 144 PROMPT 145 STO 40 146 * 147 STO 41 148 CLA 149 "PSHP=" 150 ARCL X

151 AVIEW 152 STOP 153 CLX 154+LBL "FF" 155 FS? 93 156 GTO 92 157 "POHER?" 158 PROMPT 159 X=0? 160 GTO 01 161 XEQ "DA" 162 GTO 92 163+LBL 01 164 "RSHP= ?" 165 PROMPT 166 GTO 03 167+LBL 92 168 RCL 37 169+LBL 93 178 RCL 48 171 1 172 -173 .1 174 * 175 1.03 176 + 177 * 178 19 179 + 180 RCL 41 181 + 182 RCL 38 183 * 184 CL9 185 "WF=" 186 ARCL X 187 AVIEW 188 END

WEIGHT

1. Purpose

This program computes the estimated total weight of an installed engine plus the weight of fuel consumed for a design mission profile by a helicopter with that engine(s) installed. The fuel weight calculation requires computation of maximum endurance velocity and the power associated with operation at both cruise and maximum endurance velocities. The program offers the option of direct input of rotor shaft horsepower required (previously computed by the user) or the use of program "POWER" to calculate the required power using a velocity input. The user must already have determined the maximum endurance velocity in either case. Program "VE" can be used in conjunction with "POWER" for this purpose. "POWER" is to be used, it must be executed first so that geometric data for the helicopter may be calculated. "WEIGHT" enters program "POWER" at subroutine "DA" so that the correct altitude and temperature for the design may be selected as well as to save computation time. "WEIGHT" also utilizes subroutine "OPCON" from program "FUELFL" to calculate fuel flow rates. The calculated values are displayed as follows:

Display:

Explanation:

WEI =

Weight of engine-installed (lb)

FL WT =

Fuel weight for mission (lb)

$$WTT =$$

Total weight of installed engine plus mission fuel (1b)

2. Equations

$$W_{EI} = 45 + 1.2 \cdot W_{ED}$$

$$W_{tf} = .05 W_{f} < NRP > + \frac{MAX RANGE}{V_{CRUISE}} (W_{f} < V_{CRUISE} >)$$

+ .25
$$W_f < V_{END} >$$
 + .05 $W_f < NRP >$

$$W_{tt} = W_{EI} + W_{tf}$$

$$W_{r} = (PSHP + ESHP)\hat{\beta}$$

where:

WED is the engine dry weight (1b)

WEI is the engine installed weight (estimated) (1b)

Wtf is the total fuel weight for the mission

Wtt is the total weight of installed engine plus

mission fuel (lb)

V_{CRUISE} is the specification cruise velocity (KTS)

PSHP is the shaft horsepower required at zero

velocity (phantom shp)

is the fuel flow rate of the engine at normal W_f<NRP>

rated power (lb/hr)

W_f < V_{CRUISE} > is the fuel flow rate of the engine at cruise

velocity (lb/hr)

 $W < V_{END} >$ is the fuel flow rate of the engine at maximum

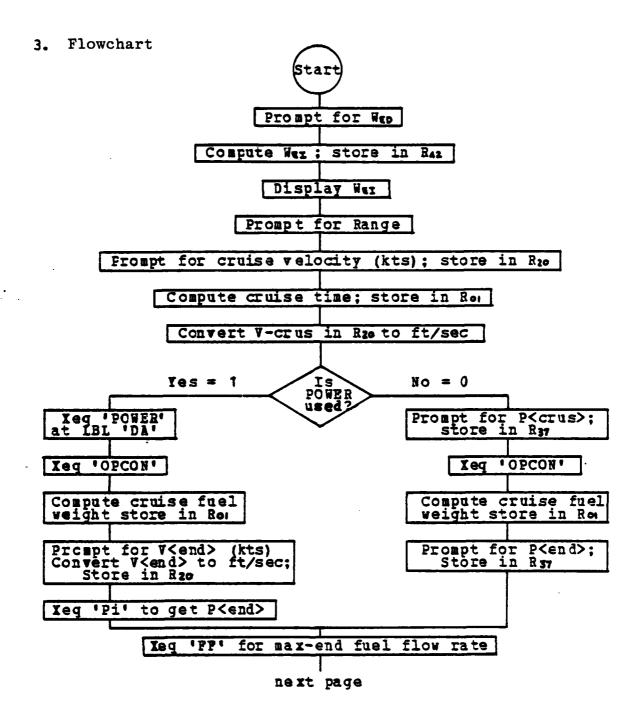
endurance velocity (lb/hr)

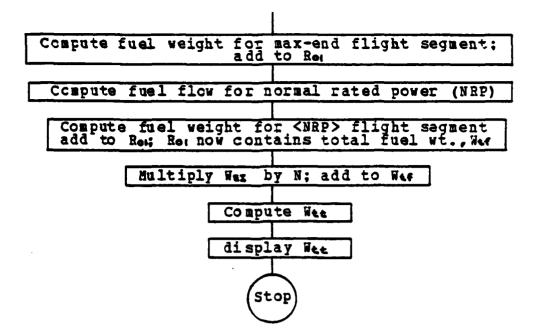
Wf is fuel flow rate (general) (lb/hr)

ESHP is engine shaft horsepower (hp)

is the slope of the fuel flow line for the

engine





and the second of the second o

The state of the s

4. Example Problem and User Instructions

Find the total weight of the installed engine plus fuel weight for the preliminary design of a helicopter under the following conditions:

WED = 400 lb

Operating Conditions:

Range = 350 nm

PA = 0

V<crus> = 100 kts; P<crus> = 531.87 shp

T = 59 F

V < end > = 58 kts; P < end > = 383.42 shp

Note: If it has not already been done, execute program "FUELFL" now using the engine data included with the "FUELFL" sample problem.

a. Assume "POWER" will not be used:

Keystrokes: Display:

(XEQ) (ALPHA) WEIGHT (ALPHA) WED=?

400 (R/S) WEI = 525.0

(R/S) RANGE=?

350 (R/S) V<CRUS>=?

100 (R/S) POWER?

O(R/S) P<CRUS>=?

531.87 (R/S) PA FT ?

O(R/S) T(F)?

59 (R/S) ZHI = 135.2

(R/S) N = ?

2 (R/S) PSHP = 685.46

(R/S) WF = 511.90

P < END > = ?

383.42 (R/S) WF = 445.67 FL WT = 1930.37 (R/S) WTT = 2980.37

b. If "POWER" is loaded and executed using the sample helicopter design data included as an example with the "POWER" user instructions, run "WEIGHT" again with the same engines and operating conditions.

Keystrokes:

(XEQ) (ALPHA) WEIGHT (ALPHA)	WED=?
400 (R/S)	WEI = 525.0
(R/S)	RANGE=?
350 (R/S)	V-CRUS=?
100 (R/S)	POWER?
1 (R/S)	PA=?
0 (R/S)	T(F)=?
59 (R/S)	PA FT ?
0 (R/S)	T(F) ?
59 (R/S)	ZHI = 135.2
(R/S)	N = ?
2 (R/S)	PSHP = 685.46
(R/S)	WF = 511.90
	V <end>=?</end>
58(R/S)	WF = 445.67
	FL WT = 1930.36
(R/S)	WTT = 2980.36

5. Programs and Subroutines Used

"FUELFL" (entered at subroutine "OPCON" or "FF")
"POWER" (OPTIONAL)

6. Storage Register Utilization Table VI shows specific storage register contents.

TABLE VI
Weight Storage Register Utilization

Storage Register	Stored Quantity
01	W _{tf} - total fuel weight for mission profile (1b)
02	δ - ratio of pressure to standard sea level pressure
03	$\sqrt{\theta}$ - square root of the ratio of absolute temperature to SSL absolute temperature
42	W _{EI} - estimated engine installed weight (lb)

Note: programs "FUELFL" and "POWER" utilize registers 00-41. The quantities stored in registers 01-03 above are lost after the execution of "WEIGHT."

7. Program Listings

RI+LBL "WEIGHT" 62 SF 03 03 "MED=?" 84 PROMPT 95 1.2 86 * 97 45 98 + **89** STO 42 18 "WEI =" 11 ARCL X 12 AVIEW 13 STOP 14 "RANGE?" 15 PROMPT 16 "V-CRUS?" 17 PROMPT 18 STO 20 19 / 29 STO 91 21 1.68889 22 ST* 29 23 "POWER?" 24 PROMPT 25 X=9? 26 GTO 91 27 XEQ "DA" 28 XEQ TOPCONT 29 PSE 30 RCL 01 31 * 32 STO 01 33 "Y-END?" 34 PROMPT 35 1.68889 36 * 37 STO 20 38 XEQ *PI* 39 GTO 92 40+LBL 91 41 *P(CRUS)?*

42 PROMPT 43 STO 37 44 XEQ "OPCON" 45 PSE 46 RCL 01 47 * 48 STO 81 49 *P(END)?* 50 PROMPT 51 STO 37 52+LBL 82 53 XEQ "FF" 54 PSE 55 .25 56 * 57 ST+ 01 58 RCL 94 59 RCL 40 60 * 61 RCL 41 62 + 63 RCL 38 64 * 65 .1 66 * 67 ST+ 01 68 CF 03 69 RCL 81 78 "FL WT=" 71 ARCL X 72 AVIEW 73 STOP 74 RCL 42 75 RCL 40 76 * 77 + 78 "MTT=" 79 ARCL X 88 AVIEW 81 END

APPENDIX D

FORTRAN ENGINE OPTIMIZER

This appendix contains an interactive computer program written to optimize the selection of a turboshaft engine for the preliminary design of a helicopter. The program is written in FORTRAN and implemented on the IBM 3033 computer. Optimization is accomplished by the selection of the powerplant which results in the minimum total weight of installed engine(s) and fuel for a specific mission profile. mission profile used for calculation of fuel weight is taken from the Helicopter Design Manual by Stephen G. Kee [Ref. 1] and represents a typical design flight profile. Computation of fuel flow characteristics is based upon equations developed in Chapter 14 of [Ref. 22] but also include a 5 percent increase in the engine manufacturer's published fuel flow This procedure coincides with preliminary design data. criteria established for military helicopters [Ref. 2].

The program uses data which must first be generated by the user using the Helicopter Power Computation Package [Ref. 21]. This data provides rotor shaft horsepower required for the specific helicopter being designed.

This program accomplishes the same results as the programs developed for use on the hand-held calculator

(Appendix C), but it has three main advantages over those programs:

- 1. Much less computation time.
- 2. Neat, hard copy output.
- 3. Up to five engines may be compared and an optimum engine selected.

A. PURPOSE

The program allows the user to rapidly calculate the fuel flow rate of an engine (or engines) for any power setting (or velocity from hover to maximum velocity) desired, at any temperature and altitude up to 36,000 feet. The only engine performance data required from the user for these calculations are the standard sea level shaft horse-power available and fuel consumption at military, normal, and cruise power settings (Appendix B). The program also provides a method of engine selection based upon weight of installed engine and mission fuel. This optimization may then be used in conjunction with cost analysis to make a final selection of the powerplant to be used in the design.

B. INPUT REQUIRED

- 1. Specific fuel consumption and engine shaft horsepower available at standard sea level conditions at normal, military, and cruise power settings.
- 2. Manufacturer's engine dry weight in pounds.
- 3. Pressure altitude in feet and temperature in degrees fahrenheit.
- 4. Number of engines to be used in the helicopter design.

- 5. Required rotor shaft horsepower (RSHP) or velocity in knots for the RSHP at which the fuel flow rate is to be computed.
- 6. Design maximum range.
- 7. Design cruise velocity.

C. OUTPUT

はいていたなから、これにおいて、これが対象と

See sample problem data output. Note: SFC are increased by 5 percent in the output data.

D. EXAMPLE PROBLEM AND USER INSTRUCTIONS

1. Input the basic helicopter design parameters using EXEC "HPLINK" (use of this EXEC file is quite simple and is explained in detail in [Ref. 21]). For this example use the following design parameters:

Main Rotor	Tail Rotor	<u>Aircraft</u>
C = 1.5 ft	C = 0.50 ft	L <tail> = 23.50 ft</tail>
R = 20.0 ft	R = 3.00 ft	W <gross> = 7,000 lbs</gross>
b = 4	b = 2	F.P.A.(FF) = 21.2
CdO = 0.01	CdO = 0.014	Vmax = 120 kts
RPM = 296	RPM = 1332	

Environmental: PA = 4000 ft

T = 95 F (design conditions)

The above procedure results in the creation of file
"HPWRPIP DATA" on the user's disk. This file contains
rotor power requirements in level flight for the helicopter being designed.

2. From CMS run program "FUELFLO" FORTRAN by typing: Global Txtlib Fortmod2 Mod2eeh Nonimsl Load FUELFLO (START Note: No file definitions (FILEDEF) are necessary, the program defines read and write files internally.

3. Respond to interactive prompts written on the terminal screen. Use the following data:

	En	gine	1	
--	----	------	---	--

	SHP	SFC
Military	1561	.46
Normal	1310	.47
Cruise	989	.51

Dry Weight: 423 lb

Pressure altitude: 4000 ft

Temperature: 95 F

Number of engines in powerplant, N: 2

Select the velocity option (option 2) for determination of Rotor Shaft Horsepower Required (RSHP) for the fuel flow rate calculation; then use:

Velocity: 75 kts

Select "N" to skip computation for different conditions or engine.

Select "Y" to compute the mission fuel weight; use:

Range: 350 nm

Cruise Velocity: 100 kts

Select "Y" to compare a second engine; use the following

data:

--- Engine 2 ---

	SHP	SFC
Military	1561	.46
Normal	1310	.47
Cruise	1000	.55

Dry Weight: 375 lb

Number of engines in powerplant, N: 2

Select "N" (No) to skip additional engine comparison. The optimum engine selection will be displayed and the program terminated.

4. Hard copy results will be available in file "FUELFLO DATA" which is created by the program onto the user's disk. A copy of this file is presented in paragraph F below.

E. ALGORITHM

Algorithm FUELFLO

Read helicopter design and power required data

Assign engine number

Write user instructions

Prompt for engine data

Prompt for engine SSL performance characteristics

Check SFC < 1.0

Reenter SFC if not < 1.0

Check SHP > 1.0

Reenter SHP if not > 1.0

Prompt for engine dry weight

Calculate slope of fuel flow line and the zero horsepower increment (SSL)

Call subroutine FUELSL

Output engine SSL data

Do if J = 1

TARA A MANAGARAN TO SERVICE TO SEASON TO SEASO

Input PA and T

Calculate pressure and temperature ratios

Call PRATIO

Call TRATIO

End Do

Input number of engines to be used in the helicopter

Calculate zero horsepower intercept at operating conditions

Calculate the zero velocity horsepower (Phantom SHP) at operating conditions.

Call ZVHP

Call ZHIALT

If J = 1

Input rotor power requirement

RSHP directly

Else

Velocity at which RSHP desired

Check that PA and T are the same for power calculations as those at which the engine is being evaluated; if not print a caution message Get RSHP from "HPWRPIP DATA"

Else use power required entered for engine 1
Calculate fuel flow rate at operating conditions

Call FLOALT

Output fuel flow data

Give options for doing additional fuel flow calculations

If desired, calculate fuel flow rate with different

PA and T

If desired, calculate fuel flow rate with a different engine

Calculate fuel weight for the mission profile

If J = 1

Input design maximum range

Input design cruise velocity

Else use range and cruise velocity previously entered
Read cruise power required from "HPWRPIP DATA"

Calculate maximum endurance velocity and rotor power
required

Call MAXEND

Calculate the zero horsepower intercept at the conditions used for power required calculations

Call PRATIO

Call TRATIO

Call ZHIALT

Calculate the zero velocity shaft horsepower (phantom SHP)

Call ZVSHP

Calculate fuel flow rates at cruise and maximum endurance velocities and at normal rated power

Compute fuel flow rate using normal rated power required

Call FLOALT using cruise power required

Call FLOALT using max endurance power required

Calculate total fuel weight

Call FUELW8 (Fuelwt)

Call ENGWT (W_{ET})

Calculate estimated installed engine weight

Calculate total weight of powerplant plus mission

 $W_{tt} = n(W_{EI}) + Fuelwt$

Output mission profile data

If J<5

fuel

Give option to try another engine

If yes

Return above and prompt for engine data
Run through program again

Else continue

If J>1

Determine the powerplant with the minimum total weight of engines plus fuel

Output recommendation for engine selection

End FUELFLO

F. PROGRAM RESULTS

** ** ** ** * * * ENGINE FUEL FLOW AND OFTIMIZATION **** ** ***

----- ENGINE 1 DATA -----

SHP SFC

MILITARY 1561.00 0.4830 NORMAL 1310.00 0.4935

CRUISE 989.00 0.5355

DRY WEIGHT: 423.0 LES

BETA: 0.3948

ALPHA: 135.32 LB/HR

----- FUEL FIOW RATE -----

PA: 4000.0 FT N: 2

TEMP: 95.0 F 'PSHP: 612.21 SHP

ZHI: 120.86 LB/HR RSHP: 385.70 SHP

FUEL FLOW RATE: 417.76 LB/HR

----- MISSION PROFILE CONDITIONS ------

PA: 4000. FT TEMP: 95. F

MAX RANGE: 350.00 NM

CRUISE VEL: 100 KTS CRUISE PWR REQD: 471.20 SHP

MAX END VZL: 65 KIS MAX END PWR REQD: 377.30 SHP

INSTALLED ENGINE WEIGHT < EA>: 552.60 LB

FUEL WEIGHT: 1826.80 LB

WEIGHT OF INSTALLED POWERFLANT 1 AND FUEL: 2932.00 LB

----- ENGINE 2 DATA -----

SHP

SFC

MILITARY 1561.00

0.4830

NORMAL

1310.00

0.4935

CRUISE 1000.00

0.5775

DRY WEIGHT: 375.0 LES

BETA: 0.3218

ALPHA: 244.14 LB/HR

----- FUEL FLOW RATE -----

PA: 4000.0 FT

N: 2

TEMP: 95.0 F

PSHP: 1355.34 SHP

ZHI: 218.05 LB/HR

RS HP:

385.70 SHP

FUEL FLOW RATE: 579.55 LB/HR

----- MISSION PROFILE CONDITIONS -----

PA: 4000. FT

95. F

MAX RANGE: 350.CC NM

CRUISE VEL: 100 KIS CRUISE PWR REQD: 471.20 SHP

MAX END VEL: 65 KTS MAX END PWR REQD: 377.30 SHP

INSTALLED ENGINE WEIGHT < EA>: 495.00 LB

FUEL WEIGHT: 2409.25 LB

WEIGHT OF INSTALLED FOWERFLANT 2 AND FUEL: 3399.25 LB

RECOMMEND ENGINE 1 BE SELECTED

G. COMPUTER PROGRAM

```
S.L.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ន
ខ្លួ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ESPONSE
                                                                                                                                                                        AT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          RESPON
                                                                                                                                                                                                                                                                                                                                                       LIED WEIGHT OF ONE ENGINE AT KNOWN CONDITIONS
AT ALT
AT NORMAL RATED FOWER
AT CRUISE POWER
AT MAX ENDURANCE POWER
PCWERFLANT AND FUEL WEIGHT
OW AT DESIRE ALT. AND TEMP.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ENGINE NUMBER

LOGICAL CCNSTANT USED FOR INTERACTIVE RESPON
LOGICAL CCNSTANT USED FOR INTERACTIVE RESPON
NUMBER OF ENGINES
HAIN ROTOR BLADES
CPTIMUM ENGINE SELECTEL
LOGICAL VARIABLE USED FOR INTERACTIVE RESPON
TAIL ROTOR BLADES
SPECIFICATION CRUISE VELOCITY: KTS
MAXIMUM ENDURANCE VELOCITY: KTS
INCREMENT CF FORWARD SPEED FOR PRINT OUT
MAXIMUM FCRWARD VELOCITY: ATS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     TEMP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   **********
                                                                                                                                                                        ρ,
                                                                                                                                                                        EHI
                                                                                                                                                                        84
                                                                                                                                                                                                                                                                                          KNOT
                                                                                                                                                                        5
                                                                                                                         L B/HR/SHP
                                                                                                                                                                                                                                           FAHR ENHEIT
                                                                                                                                                                      AIT
                                                                                                                                                                                                                                                                                      AIRCRAFT,
                                                                                                                                                                      TY
                                                                                                                             ••
                                                                                                                                                                                  .
                                                                                                                       SUMPTION:
EPOWER
OF TEMP.
PARASITE FOWER
HAIN ECTOR RADIUS
REQUIRED FOTOR SHP
TAIL RCTOR RADIUS
SPECIFIC FUEL CONSUMPTION
ENGINE SHAFT HORS EPOHER
SOR ROOT OF RATIO OF TEMP.
IAIL ROTOR RFH
TAIL ROTOR RFH
TORU AT ALT IN DEGREES FIRM
TANGE VELOCITY
FORM ANGE VELOCITY
FUEL FIOW BATE AT KNOWN CC
FUEL FIOW BATE AT CRUISE FUEL FIOW RATE AT CRUISE FUEL FIOW RATE AT CRUISE FUEL FLOW SHE FUEL FUEL FLOW SHE FLO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INTEGERS
   SETTINE TO THE STATE OF THE STA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RESP 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LRESP
LRESP
LRESP
NNOR
NORY
VCRUS
VENUS
VENUS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ***
```

C

WRITE HEADING IF (J. GT.1) WRITE (8,590) WRITE (8,590) J WRITE (8,590) J WRITE (8,500) SHPI (1), SPCI (1) WRITE (8,620) WEDRY, BETA, ALPHA WRITE (8,620) WEDRY, BETA, ALPHA FOR SUSEQUENT ENGINES USE THE SAME PRESSURE ALTITUDE AND IF (.NOT.(J.EQ.1)) GO TO 160 IF (.NOT.(J.EQ.1)) GO TO 160 WRITE (6,630) READ (5,4) PAFT WRITE (6,650) READ (5,4) T CONTINUE CALL FRESSURE RATIO, TEMP RATIO, AND ZERO SHP INCREMENT CALL FRESSURE RATIO, TEMP RATIO, AND ZERO SHP INCREMENT CALL FRESSURE RATIO, TEMP RATIO (A.M.) CALL FRESSURE RATIO, TEMP RATIO (A.M.) CALL FRESSURE RATIO, TEMP RATIO (A.M.) CALL FRESTURE FRESSURE RATIO, TEMP RATIO, AND ZERO SHP INCREMENT
--

SINGLESS PRODUCT TOURS TO SECRETARIES WINDOWS WORLD BY WORLD BY WINDOWS IN THE SECRETARIES TO SECRETARIES AND SECRETARIES AND

!	WRITE CPTIONS PCR COING ADDITIONAL FUEL PLOW CALCULATIONS A	23
	X G.	75,
•	IF (.NOT. (NORY.EC.IRESP)) GO TO 250	5C65
2	PATINUE NORY. EQ. LRESP1) GO TO 340	700
	HRITE (6,790)	-00g
	IRY A	
0	ORY.EQ.IRESP)) GO TO 260	8400 8400
	F (NORY.EQ.LRESP1) GO TO 340	80°
0	CONTINUE	92
	FOR SUSEQUENT ENGINE COMPARISCNS, USE THE DESIGN MISSION PROFILE	000 0
	IF (.NOT. (J. EQ. 1)) GC TO 280	96
!	WRITE (6,810)	0000 0000 0000
	READ (5, 620) NORY	030
	IF (NORY.EQ.LRESP1) GO TO 340 IF (.NOT. (NORY.EQ.IRESP)) GO TO 290	2000
	A PROMPT FOR RANGE AND CRUISE VELOCITY	860
	WRITE (6,830)	25
	GE ST	100
	WRITE (6,840)	7
	READ (5,*) VCRUS	190

こここここここ	ころろろろろろろうこうりゅう	MUMUM State	Maaaaa aaaaaa	4444 4444	かいかい	いいいいい	00000000000000000000000000000000000000
CCCCCLATE V-HAX ENDURANCE AND RSHP POR V-MAX ENDURANCE CALL HAXEND (PUR, VFK, VCRUS, VHAX, PURC, PEND, VEND) 280 CONTINUE	CC CALCULATE TOTAL WEIGHT OF ENGINE AND FUEL	C CCALCULATE ZERO VEIOCITY HORSEFOWER (PHANTOM SHAFT HORSEPOWER) CALL ZVSHP (ZHIX, EFTA, N, PSHP)	CCALCULATE PUBL FLOW RATES	CCALCULATE TOTAL FUEL WEIGHT	C CCALCULATE ESTIMATED INSTALLED ENGINE WEIGHT	CCALCULATE TOTAL WEIGHT OF ENGINE AND FUEL WIOT(J)=FLOAT(N)*WEI+FUEL OF	C

650 670 670

04

202

100

800

20

りつけられているようでは、これでは、これでは、これでは、これでは、これでは、これでは、これでは、これ														
00000	लिल	医阿阿萨	សមាស	ខាមា	r 'Se (Se (Se	. G. G. G	r D r D r D	P- GP- D	در الله الكبر (ადიიი	ဗဗဗ	9000	900000	9
SCRT((T, + 459.688)/518.688)	CBROUTIN	SUBROUTINE ZHIAIT (AIPHA, DELTA, STHETA, ZHIX) REAL ALPHA, DELTA, STHETA, ZHIX	ZHIX=Alpha*delta*stheta	RETURN	SUBROUTINE Z	SUBROUTINE ZVSHP (ZHIX, BETA, N, FSHP)	REAL BETA, PSHP, ZHIX INTEGER N	PSHP=PLOAT(N) *ZHIX/BETA	RETURN END	SUBROUTINE FLOALT: CALCULATES THE FUEL FLOW RATE AT OPERATING CONDITIONS FOR A GIVEN TOTAL ROTOR SHAFT HURS FOURED BY THE AIRCRAFT.	SUBROUTINE FLOALT (RSHPMX, BETA, N, PSHP, WFALT)	REAL BETA, ESHP, PSHP, RSHPM X, WFAIT INTEGER N	(FLOAT (N) - G	

			ן המתמתמתמתמת בעשבעפרפפ <u>סבדל</u>
WEALT= (PSHP + ESHP) * BETA C RETURN C	SUBROU REAL INTEGE FUELET	180 180 1	C SUBROUTINE MAXENC: CALCULATES V-MAX EN DURANCE AND RSHP FOR C SUBROUTINE MAXEND (PWR, VFK, VCRUS, VMAX, PWRC, PEND, VEND) C REAL PWR (200), VPK (200), PW RC, PEND INTEGER 1, VCR US, VMAX, VEND C I = VCRUS PWRC=PWR (I+1)

```
Vend=VFK (2)
PEND=PWR (2)
DO 20 I=2.VMAX
IF (.NOT. PWR (I). IE. PWR (I-1) ) GO TO 20
IF (.NOT. PWR (I). IE. FWR (I+1) ) GO TO 10
VEND=VFK (I)
PEND=PWR (I)
CONTINUE
CONTINUE
RETURN
```

AND LEGIS VINE EXCENSES EXCESSES RECENT FOR THE FORMAR SERVING SERVING

APPENDIX E

HELICOPTER POWER CALCULATIONS FOR THE HP-41C

This appendix contains 3 programs developed for use with the HP-41C programmable calculator. They are:

- 1. "POWER" which computes the total rotor shaft horsepower required for a helicopter in forward flight or hover.
- 2. "VE" which utilizes "POWER" to calculate the maximum endurance velocity and power required at that velocity.
- 3. "VMR" which utilizes "POWER" to calculate the maximum range velocity and power required at that velocity.

POWER

1. Purpose

This program calculates the total power of a helicopter in hover or in forward flight. It links 13 basic subroutines developed in [Ref. 24] into a single program to enable quick calculation of total power after one initial input of the basic helicopter design data.

- a. The program features are:
 - (1) One input of design data.
 - (2) Ability to change PA, T, and V rapidly for repetitive calculations.
 - (3) Single output: Total power required with tip loss.
 - (4) Incorporation of main rotor and tail rotor calculations in each subroutine.
 - (5) Easy access by other programs for calculation of power required.
 - (6) Designed for iterative use (e.g. calculation of maximum endurance velocity or determination of many points to generate power curve),
 - (7) Intermediate design and performance values (such as disk area or profile power) are stored and easily accessed if needed.
- b. The program limitations are:
 - (1) Only a rectangular rotor blade may be used (or equivalent chord separately calculated).
 - (2) Only hover and forward flight powers may be calculated (climbing flight is not included).
 - (3) All calculations are for an out of ground effect condition.

- c. The basic programming technique used is to combine main rotor and tail rotor calculations into single subroutines by one of two methods (depending upon which used the fewest bytes of program memory):
 - (1) Calculation of the main rotor characteristic (e.g. solidity) then calculation of the corresponding tail rotor characteristic separately.
 - (2) Calculation of the main rotor characteristic (e.g. tip loss factor, B), continuation of program and calculation of tail rotor thrust (which requires main rotor total power to be first computed). Then flag 02 is set and program execution is returned to the subroutines where the tail rotor characteristics are calculated. In these subroutines, the same equation steps as those for the main rotor are used but tail rotor values are recalled for the computations. The flag 02 tells each subroutine to use tail rotor values.

The calculated value of total power required is displayed as follows:

Display:

Explanation:

PT =

Helicopter total rotor shaft horsepower required (out of ground effect with tip losses)

2. Equations

All equations were taken directly from [Ref. 24]. Tip loss is assumed in the calculation of induced power and all calculations are for an out of ground effect condition. The basic equations used in each subroutine are listed below.

a. Equations used twice in each subroutine; once for the main rotor and once for the tail rotor:

$$A_{D} = \pi R^{2}$$

$$\nabla_{T} = \Omega R$$

$$\nabla_{T} = \frac{T}{A_{D} \rho V_{T}^{2}}$$

$$B = 1 - \frac{\sqrt{2C_T}}{b}$$

$$v_i = \left[\frac{T}{2\rho A_D}\right]^{\frac{1}{2}}$$

$$v_{i_f} = \frac{-V_f^2}{2v_i^2} + \left[\frac{V_f^2}{2v_i^2}\right]^{\frac{1}{2}} v_{i}$$

$$P_{i_{TL}} = \frac{T}{B}$$

$$P_{O} = \frac{1}{8} \sigma \overline{C}_{dO} \rho A_{D} V_{T}^{3} \left[1 + 4.3 \frac{V_{f}^{2}}{V_{T}} \right]$$

b. Main rotor only:

$$P_{p} = \frac{1}{2} \rho f_{f} V_{f}^{3}$$

$$P_{T_{MR}} = P_{i_{MR}} + P_{o_{MR}} + P_{p}$$

$$T_{MR} = W$$

. Tail rotor only:

$$T_{tr} = \frac{P_{TMR}}{\Omega_{MR} \ell_{tr}}$$

d. Operating conditions:

$$h_{o} = \frac{1 - \left[\frac{T_{SSL}}{T} - 1 - K_{1}h_{p}\right]^{\cdot 23496}}{K_{1}}$$

$$\rho = \rho_{SSL}[1 - (K_1 h_{\rho})]^{4.2561}$$

e. Total Power:

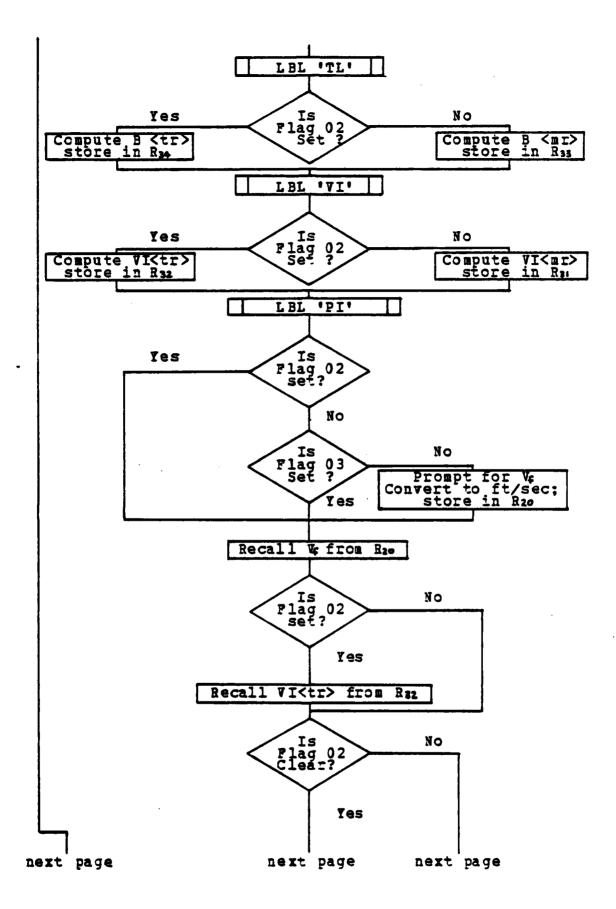
where:

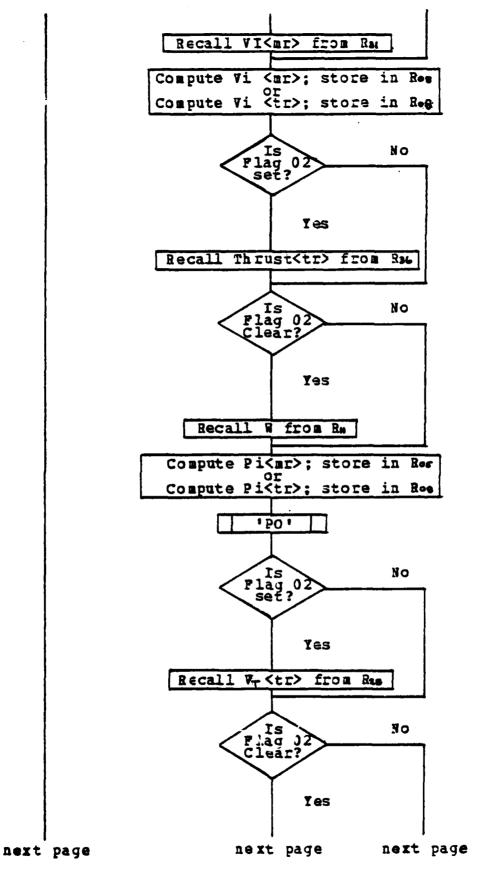
$$A_{D}$$
 is the disk area (ft)

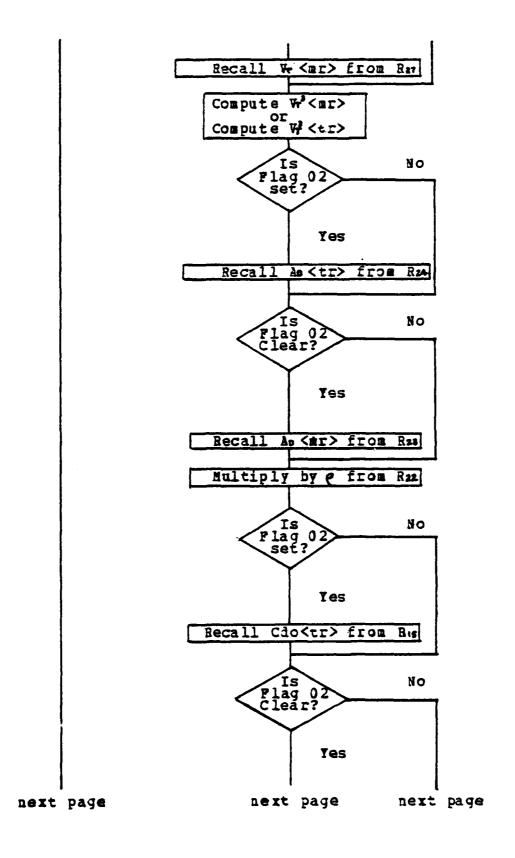
```
C
              is the rotor chord (ft)
              is the number of rotor blades
\mathbf{v}_{\mathbf{T}}
              is the rotor tip velocity (ft/sec)
Ω
              is the rotational velocity of the rotor (rad/sec)
^{\text{C}}_{\mathbf{T}}
              is the coefficient of thrust
              is the thrust required for the tail rotor (lb)
              is the air density (slugs/ft)
              is the tiploss factor
vi
              is the induced velocity (ft/sec)
Vif
              is the induced velocity in forward flight (ft/sec)
V
              is the forward velocity (ft/sec)
Pi_{TL}
              is the induced power required with tip loss (hp)
Po
              is the profile power required (hp)
CdO
              is the profile drag coefficient
Pp
              is the parasite power required (hp)
              is the equivalent flat plate area in forward
f
              flight (ft)
              is the total power required by the main rotor (hp)
\mathbf{T}_{\mathbf{MR}}
              is the thrust of the main rotor (lb)
              is the gross weight (lb)
1<sub>tr</sub>
              is the distance between tail rotor hub and main
              rotor mast (ft)
              is the density altitude (ft)
T
              is temperature (absolute)
^{\mathrm{T}}SSL
              is the standard sea level temperature (absolute)
              is a constant = 6.875 \times 10^{-6}
K<sub>1</sub>
              is pressure altitude (ft)
```

THE RESIDENCE AND STREET AND STRE

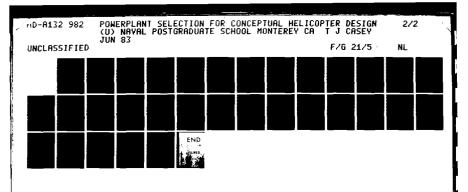
3. Flowchart Star Prompt for and input Helo Data Store in Roo - R17 LBL 'AREA' Compute A. <mr>; store in R23 Compute Ao ; store in R24 LBL 'SD' Compute or <mr>; store in Ras Compute o ; store in Ra6 LBL 'VT' Compute VT <mr>; store in R27 Compute VT ; store in R29 LBL. DA. Prompt for PA (ft); store in Rie Prompt for T (F); store in Ris Compute DA; store in Rai LBL 'DEN' Compute air density; store in R22 LBL 'CT' Is Flag 02 Set 2 Yes No Compute Cr
store in R30 Compute CT <mr>
store in Ree next page next page

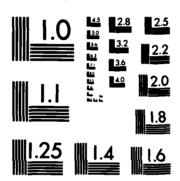






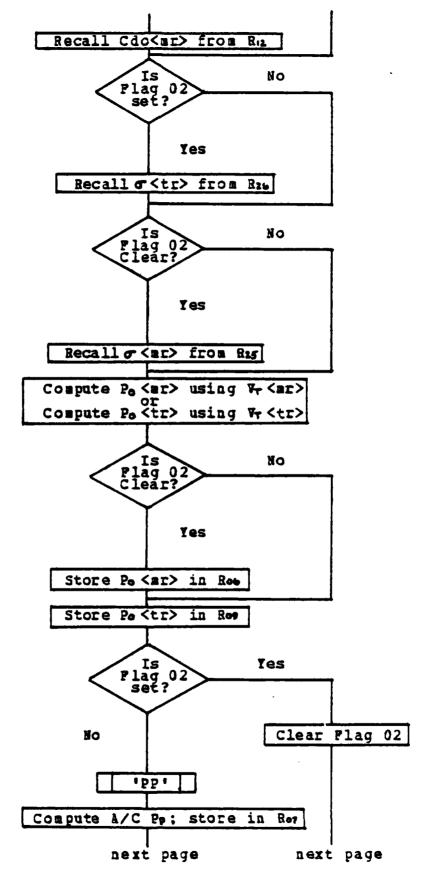
BASKSING KOOD COM TO THE



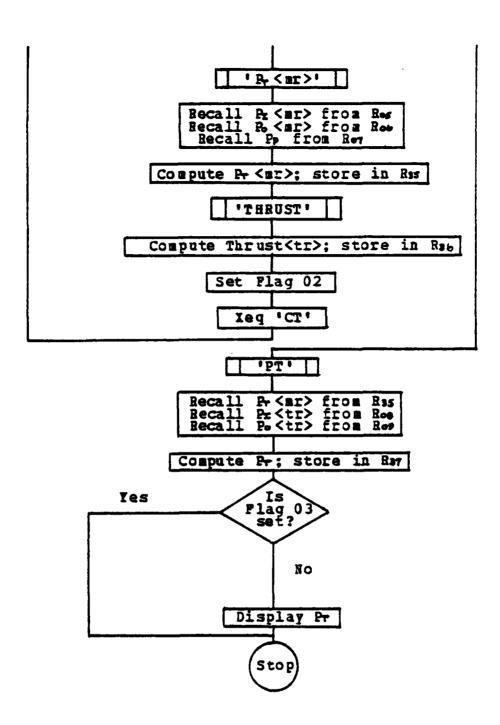


MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANDARDS-1963-A

AND THE PROPERTY OF THE PROPERTY AND THE PROPERTY AND THE PROPERTY OF THE PROP



next page



4. Example Problem and User Instructions

Find the total rotor power required for a helicopter under the following conditions:

Main Rotor	Tail Rotor	<u>Aircraft</u>
C = 1.50 ft	C = 0.50 ft	L <tail> = 23.50 ft</tail>
R = 20.0 ft	R = 3.00 ft	W <gross> = 7,000 lbs</gross>
b = 4	b = 2	F.P.A.(FF) = 21.2
CdO = 0.01	CdO = 0.014	VF = 0 kts (hover)
RV = 31 rad/sec	RV = 139.5 rad/sec	
Environmental: PA	T = 0 ft $T = 59$ F	(standard sea level)
Keystrokes:		Display:
(XEQ) (ALPHA) POWE	CR (ALPHA)	HELO DATA
(R/S)		W=?
7000.0 (R/S)		RV(mr)=?
31.0 (R/S)		b(mr)=?
4 (R/S)		C(mr)=?
1.50 (R/S)		CdO(mr)=?
0.01 (R/S)		R(mr)=?
20.0 (R/S)		F.P.A.(FF)=?
21.2 (R/S)		RV(tr)=?
31 (R/S)		b(tr)=?
2 (R/S)		C(tr)=?
0.50 (R/S)		CdO(tr)=?
0.014 (R/S)		R(tr)=?
3.00 (R/S)		L <tail>=?</tail>
23.50 (R/S)		PA=?

0.0 (R/S)

59.0 (R/S) VF=?

0 (R/S) PT = 660.08

To calculate the power required at a different V for the same helicopter at the same altitude and temperature, execute "PI" with:

T=?

VF = 100 kts

Keystrokes: Display:

(XEQ) (ALPHA) PI (ALPHA) VF = ?

100 (R/S) PT = 531.87

To calculate the power required at any V for the same helicopter at a different altitude and temperature, execute "DA" with:

VF = 100 kts

PA = 4000 ft

T = 95 F

Keystrokes: Display:

(XEQ) (ALPHA) DA (ALPHA) PA = ?

4000 (R/S) T = ?

95 (R/S) VF = ?

100 (R/S) PT = 471.22

5. Programs and Subroutines Used

"POWER"

"AREA" calculates Disk Area

"SD" calculates Solidity

"VT" calculates Rotor Tip Velocity

"DA" calculates Density Altitude

"DEN" calculates Air Density

"CT" calculates Coefficient of Thrust

"TL" calculates Tip Loss Factor

"VI" calculates Induced Velocity

"PI" calculates Profile Power with tip loss OGE

"PO" calculates Profile Power

"PP" calculates Parasite Power

"PT" calculates Total Main Rotor Power

"THRUST" calculates Tail Rotor Thrust required

"PT" calculates Total Power required

6. Storage Register Utilization

Table VII and VIII show specific storage register contents.

Note: Registers 00-09 are considered temporary and are also used by other programs.

TABLE VII

POWER Storage Register Utilization: 00-19

Storage	
Register	Stored Quantity
00	C _{MR} - main rotor chord (ft)
01	R _{MP} - main rotor radius (ft)
02	Ω _{MR} - rotational velocity of the main rotor (radians/sec)
03	C _{tr} - tail rotor chord (ft)
04	R _{tr} - tail rotor radius (ft)
05	P - main rotor induced power with tip MR losses (hp)
06	PomR - main rotor profile power (hp)
07	P _n - parasite power (hp)
08	P _i - tail rotor induced power with tip tr losses (hp)
09	P - tail rotor profile power (hp)
10	b _{MR} - the number of main rotor blades
11	W - the weight of the helicopter
12	$\overline{C}_{\mbox{do}_{\mbox{MR}}}$ - the average profile drag coefficient for the main rotor
13	<pre>f - the equivalent flat plate area for forward flight calculations (ft)</pre>
14	b _{tr} - the number of tail rotor blades
15	- the average profile drag coefficient for the tail rotor
16	<pre>1 - the length of the tail, from main rotor hub to the tail rotor hub (ft)</pre>
17	Ω_{tr} - rotational velocity of the tail rotor (radians/sec)
18	T - outside air temperature in degrees F
19	h _p - pressure altitude (ft)
L	

TABLE VIII

POWER Storage Register Utilization: 20-37

Storage Register	Stored Quantity
20	V _r - forward velocity (ft/sec)
21	h - density altitude (ft)
22	ρ - air density (slugs/ft)
23	$A_{D_{MR}}$ - the main rotor disk area (ft)
24	ADtr - the tail rotor disk area (ft)
27	$V_{T_{MR}}$ - velocity of the main rotor tip (ft/sec)
28	$V_{T_{tr}}$ - velocity of the tail rotor tip (ft/sec)
29	$C_{\begin{subarray}{c} T \\ \end{subarray}}$ - the coefficient of thrust for the main rotor
30	C _T - the coefficient of thrust for the tail rotor
31	V - induced velocity of the main rotor (ft/sec)
32	V - induced velocity of the tail rotor (ft/sec)
33	B _{MR} - the tip loss factor for the main rotor
34	B _{tr} - the tip loss factor for the tail rotor
35	P _T - the total power required for the main mr rotor (hp)
36	T _{tr} - thrust required for the tail rotor (ft-lb/sec)
37	P _T - total power required for the helicopter (hp)
l	

PERSONAL CARREST CARREST CARREST AND CARREST C

7. Program Listings

e1+LBL "POMER"	51 RCL 94	101 32
82 "HELU DATA"	52 X+2	102 -
93 AVIEN 94 STOP	go Li	103 .5555
94 STOP	54 *	194 *
	55 STO 24	105 273.16
A6 PROMPT	56 CLX	106 +
07 STO 11	57+LBL "SD"	107 /
07 STO 11 08 *RV <mr>=?*</mr>	58 RCL 10	108 288.16
99 PROMPT	59 RCL 90	109 +
10 STO 17	60 *	110 .23496
10 STO 17 11 *b <nr>=?*</nr>	61 RCL 01	111 Y † X
12 PROMPT	62 /	112 CHS
13 STO 10	63 PI	113 1
14 "C <mr>=?"</mr>	64 /	114 +
15 PROMPT	65 STO 25	115 6.875 E-06
16 STO 90	66 CLX	116 /
17 "CdO(MR)=?"	67 RCL 14	117 STO 21
10 DDAMPT	68 RCL 03	118+LBL "DEN"
19 STO 12		119 RCL 21
28 "R <nr>=?"</nr>	79 RCL 04	120 6.875 E-96
21 PROMPT	69 * 70 RCL 04 71 /	121 *
22 STO 01	72 PI	122 CHS
23 "F.P.A(FF)=?"	73 /	123 1
24 PROMPT	74 STO 26	124 +
25 STO 13	74 STO 26 75 CLX	125 ENTERT
24 PROMPT 25 STO 13 26 "RY <tr>=?" 27 PROMPT 28 STO 02 29 "b<tr>=?" 79 PROMPT</tr></tr>	76+LBL "YT"	126 4.2561
27 PROMPT	77 RCL 01	127 Y 1 X
28 STO 92	78 RCL 17	128 .0023769
29 *b(TR)=?*	79 *	129 *
30 PROMPT	80 STO 27	130 STO 22
31 STO 14	81 CLX	131 CLX
32 *C(TR)=?*	82 RCL 84	132+LBL "CT"
33 PROMPT	33 RCL 02	133 FS? 02
34 STO 03	84 *	134 GTO 97
35 *CdO(TR)=?*	85 STO 28	135 RCL 11
	36 CLX	136 RCL 23
37 STO 15	97+LBL "DA"	137 🗸
36 PROMPT 37 STO 15 38 *R <tr>=?* 39 PROMPT</tr>	88 -PA =? -	138 RCL 22
39 PROMPT	89 PROMPT	139 /
40 STO 84	90 STO 19	140 RCL 27
41 "L <tail>=?"</tail>	91 6.875 E- 0 6	141 X†2
42 PROMPT	92 *	142 /
43 STO 16	93 CHS	143 STO 29
44+LBL "AREA"	94 1	144 GTO 98
45 RCL 81	95 +	145+LBL 07
46 X12	96 5.2561	146 RCL 36
47 PI	97 Y 1 X	147 RCL 24
48 *	98 "T(F)=?"	148 /
49 STO 23	99 PROMPT	149 RCL 22
50 CLX	100 STO 18	150 /
AA ABII		

```
151 RCL 28
                          201 /
                                                       251 /
152 X+2
                          202 RCL 24
                                                       252 FC? 02
153 /
                          203 /
                                                       253 STO 05
154 STO 39
                          204 SQRT
                                                       254 STO 88
                          285 ST0 32
155+LBL 98
                                                       255+LBL "PO"
                          206+LBL 12
156 CLX
                                                       256 FS? 92
157+LBL "TL"
                          207+LBL "PI"
                                                      257 RCL 28
158 FS? 02
                          208 FS? 02
                                                       258 FC? 92
                          209 GTO a
159 GTO 99
                                                       259 RCL 27
160 RCL 29
                         210 FS? 03
                                                       260 3
161 2
                          211 GTO a
                                                       261 Y#X
                          212 *VF=?*
                                                       262 FS? 82
162 *
                          213 PROMPT
163 SORT
                                                       263 RCL 24
                         214 1.68889
164 RCL 10
                                                       264 FC? 92
165 /
                          215 *
                                                       265 RCL 23
166 CHS
                          216 STO 29
                                                       266 *
167 1
                          217+LBL a
                                                       267 RCL 22
168 +
                          218 RCL 20
                                                       268 *
169 STO 33
                          219 FS? 02
                                                       269 FS? 92
                         220 RCL 32
179 GTO 10
                                                       270 RCL 15
                          221 FC? 02
171+LBL 99
                                                       271 FC? 02
                          222 RCL 31
172 RCL 30
                                                       272 RCL 12
173 2
                          223 /
                                                       273 *
174 *
                          224 X12
                                                       274 FS? 82
175 SQRT
                          225 2
                                                       275 RCL 26
176 RCL 14
                          226 /
                                                       276 FC? 92
177 /
                          227 STO 98
                                                       277 RCL 25
178 CHS
                          228 X12
                                                       278 *
179 1
                          229 1
                                                       279 4400
180 +
                         230 +
                                                       288 /
181 STO 34
                         231 SQRT
                                                       281 STO 09
182+LBL 10
                          232 RCL 08
                                                       282 RCL 20
183+LBL -YI-
                         233 -
                                                       283 FS? 82
                          234 SQRT
184 FS? 02
                                                       284 RCL 28
                          235 FS? 02
185 GTO 11
                                                       285 FC? 82
186 RCL 11
                          236 RCL 36
                                                       286 RCL 27
                          237 FC? 02
187 2
                                                       287 /
188 /
                          238 RCL 11
                                                       288 X12
189 RCL 22
                          239 *
                                                       289 4.3
198 /
                          249 FS? 82
                                                       290 *
191 RCL 23
                          241 RCL 32
                                                       291 1
192 /
                          242 FC? 82
                                                       292 +
193 SQRT
                          243 RCL 31
                                                       293 RCL 89
194 STO 31
                          244 *
                                                       294 *
195 GTO 12
                         245 550
                                                       295 FC? 82
196+LBL 11
                         246 /
                                                       296 STO 86
197 RCL 36
                         247 FS? 82
                                                       297 STO 09
198 2
                         248 RCL 34
                                                       298 FS2C 02
199 /
                          249 FC? 02
                                                       299 GTO 12
200 RCL 22
                          250 RCL 33
```

```
300+LBL -PP-
391 RCL 29
302 3
303 YtX
394 RCL 13
305 +
306 RCL 22
307 *
308 1100
309 /
310 STO 07
311+LBL "PT(MR)"
312 RCL 05
313 RCL 96
314 +
315 RCL 07
316 +
317 STO 35
318+LBL "THRUST"
319 RCL 35
329 550
321 *
322 RCL 17
323 /
324 RCL 16
325 /
326 STO 36
327 SF 02
328 XEQ "CT"
329+LBL *PT*
330+LBL 12
331 RCL 35
332 RCL 08
333 +
334 RCL 89
335 +
336 STO 37
337 FS? 03
338 GTO 13
339 -PT=-
340 ARCL X
341 AVIEW
342 STOP
343+LBL 13
344 END
```

1. Purpose

This program utilizes program "POWER" iteratively and solves for the maximum endurance velocity and power required at that velocity. The user is given the option of selecting the velocity range over which the power is calculated as well as the velocity increment to be used. Since the maximum endurance velocity for a helicopter occurs at that velocity where power required is a minimum, the program simply compares the total power required at each velocity, saves the smallest value and displays the associated velocity as that at which maximum endurance will occur. Execution of this program requires 2 minutes for ten velocity iterations. It is therefore recommended that the program be initially run at 10 knot increments over the entire velocity range from 0 to V max. The velocity displayed will be the maximum endurance velocity accurate to within \pm 5 kts. The program may then be run a second time starting 5 kts below the displayed V<end> and stopping 5 kts above it using 1 kt intervals. This procedure will enable a V<end> accurate to within 1 kt to be obtained in less than 10 minutes for almost all designs. The program output displays are as follows:

Display:

Explanation:

V<end>=

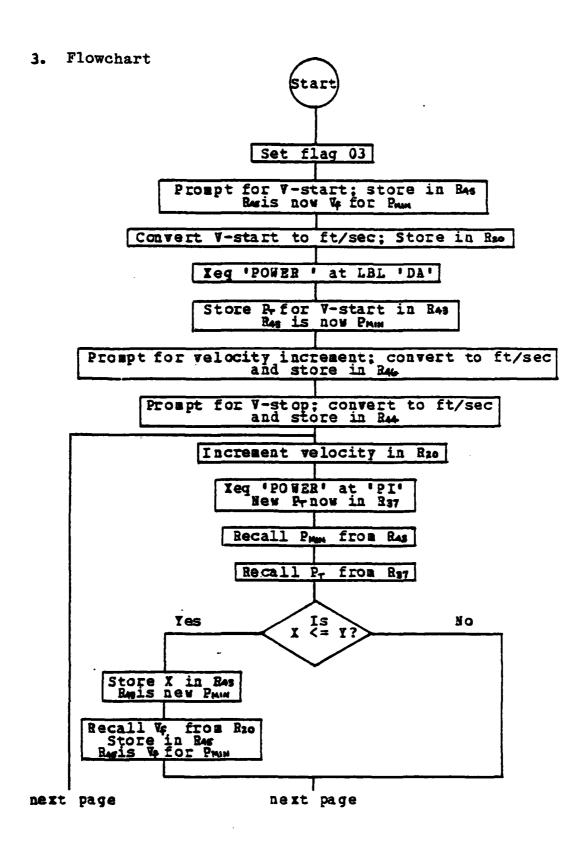
Maximum Endurance Velocity

P<V end>=

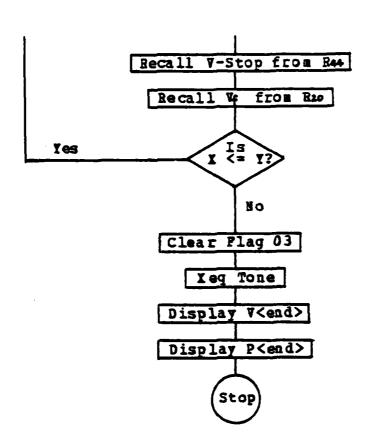
Total power required at V<end>

2. Equations

 V_f (ft/sec) = 1.6889 x V_f (knots) where: V_f is forward velocity



I december with the second of the second second



4. Example Problem and User Instructions

Find the maximum endurance velocity for the sample helicopter design used for the "POWER" example problem under the following conditions:

65 (R/S)

(R/S)

a. 10 kt increment from 0 to V<max>.

(XEQ) (ALPHA) VE (ALPHA) V-START? O (R/S) PA = ?
O(R/S) PA = ?
0 (R/S) T <f> = ?</f>
59 (R/S) INCR = ?
10 (R/S) V-STOP = ?
120 (R/S) $V < end > = 60$
(R/S) P < end > = 384
b. 1 kt increment from $V = 55$ kts to $V = 65$ kts
Keystrokes: Display:
(XEQ) (ALPHA) VE (ALPHA) V-START?
55 (R/S) PA = ?
$0 (R/S) \qquad T = ?$
59 (R/S) INCR = ?
1 (R/S) V-STOP = ?

V < end > = 58

P<V end>= 383

5. Programs and Subroutines Used

"VE"

"POWER" (entered at subroutine "DA" or "PI")

6. Storage Register Utilization

Table IX shows specific storage register contents.

TABLE IX

VE Storage Register Utilization

Storage Register	Stored Quantity
00-41	- used by "POWER"
42	- used by "WEIGHT"
43	P _T - the minimum calculated total power MIN required (hp)
44	<pre>v_B - the upper bound velocity selected for the iteration (ft/sec)</pre>
45	V _{MP} - the velocity at minimum total power required (ft/sec)
46	V _{INC} - the velocity increment selected (ft/sec)

7. Program Listings

BI+LBL "VE" 92 SF 93 93 "V-START" 84 PROMPT 95 STO 45 96 1.6889 97 * 98 STO 29 89 XEQ -50-10 570 43 11 "INCR ?" 12 PROMPT 13 1.68889 14 * 15 STO 46 16 "V-STOP?" 17 PROMPT 18 1.68889 19 * 29 ST0 44 21+LBL 13 22 RCL 46 23 ST+ 20 24 XEQ "P!" 25 RCL 43 26 RCL 37 27 84=42 28 GT0 13 29 GTO 14

36+LBL 17 31 870 43 32 CLX 33 RCL 28 34 1.68889 **35** / 36 STO 45 37+LBL 14 38 PCL 44 39 RCL 20 48 %<= 42 41 GTO 12 42 CF 03 43 TONE 2 44 RCL 45 45 FIX 0 46 "Y(END)=" 47 ARCL X 48 AVIEW 49 STOP 50 RCL 43 51 "P(END)=" 52 ARCL Y 53 AVIEW 54 END

1. Purpose

This program utilizes program "POWER" iteratively and solves for the maximum range velocity and power required at that velocity for a helicopter. The user is given the option of selecting the velocity range over which the power is calculated as well as the velocity increment to be used. The maximum range velocity for a helicopter occurs at that velocity where the ratio of power required to velocity is a minimum (considering also the zero power fuel flow or phantom SHP). The graphical method for determining the maximum range velocity is illustrated in Chapter 14 of [Ref. 20]. Program "VMR" computes the slope of a line drawn from the origin (modified to include the Phantom SHP) of the Power Required vs. Velocity curve to the power curve itself. The slope is recalculated at each velocity over the velocity range designated by the user. The program compares the slope obtained at each velocity, saves the smallest value and displays the associated velocity as that at which maximum range will occur. Execution of this program requires 2 minutes for ten velocity iterations. Since the maximum range velocity will occur above the maximum endurance velocity, it is recommended that the program be initially run at 10 knot increments over the range from V<end> to V<max>. The velocity displayed will be the maximum range velocity accurate to within ± 5 kts. The program may then

be run a second time starting 5 kts below the displayed VMR and stopping 5 kts above it using 1 kt intervals. This procedure will enable a VMR accurate to within 1 kt to be obtained in less than 10 minutes for almost all designs. The program output displays are as follows:

Display:

Explanation:

VMR=

an American Assistanti (Principles) (Principles) and and analysis

Maximum Range Velocity

P < Vmr > =

Total power required at VMR

2. Equations

 V_f (ft/sec) = 1.6889 x V_f (knots)

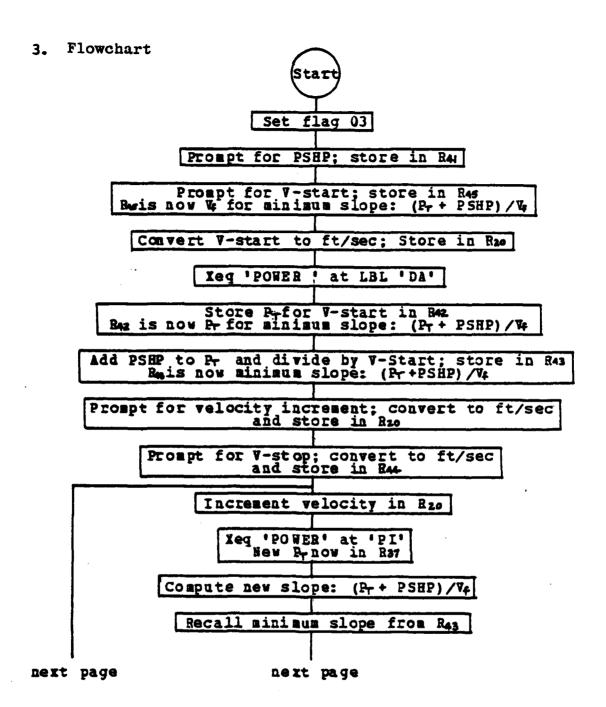
slope of tangent line = $\frac{(P_T + PSHP)}{V_f \text{ (knots)}}$

where:

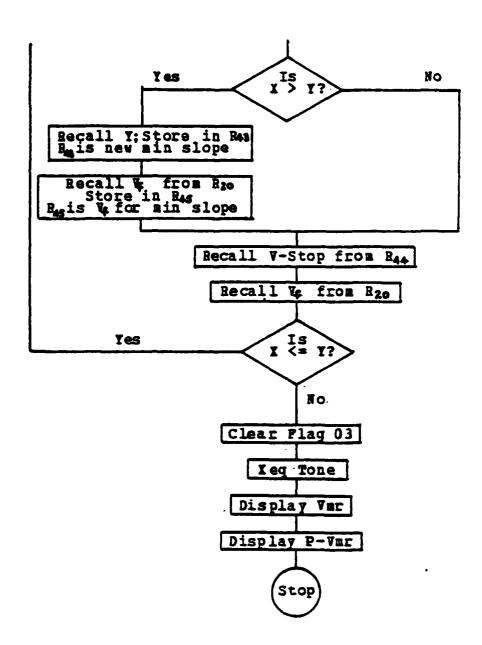
V_f is the forward velocity of the helicopter

 $\mathbf{P_T}$ is the total power required for the helicopter at a specified $\mathbf{V_f}$ (hp)

PSHP is the zero velocity shaft horsepower (phantom SHP) for the powerplant used at a specified pressure altitude and temperature (hp)



AND THE PROPERTY AND THE PROPERTY OF THE PROPE



ACCOUNT TO THE PROPERTY OF THE

4. Example Problem and User Instructions

Find the maximum range velocity for the sample helicopter design used for the "POWER" example problem under the following conditions:

PSHP = 310 SHP

V < end > = 58 kts

V<max> = 120 kts

PA = 0 ft

T = 59 F

a. 10 kt increment from V<end> to V<max>.

Keystrokes: Display:

(XEQ) (ALPHA) VMR (ALPHA) PSHP = ?

310 (R/S) V-START = ?

58 (R/S) PA = ?

 $0 (R/S) \qquad T<F> = ?$

59 (R/S) INCR = ?

10 (R/S) V-STOP = ?

120 (R/S) Vmr = 108

(R/S) P < Vmr > = 593

b. 1 kt increment from V = 103 kts to V = 113 kts.

Keystrokes: Display:

(XEQ) (ALPHA) VMR (ALPHA) PSHP = ?

310 (R/S) V-START =?

103 (R/S) PA = ?

 $0 (R/S) \qquad T<F> = ?$

59 (R/S) INCR = ?

1 (R/S)
$$V-STOP = ?$$
113 (R/S) $Vmr = 108$
(R/S) $P = 593$

5. Programs and Subroutines Used

"VMR"

"POWER" (entered at subroutine "DA" or "PI")

6. Storage Register Utilization

Table X shows specific storage register contents.

TABLE X

VMR Storage Register Utilization

Storage Register	Stored Quantity
00-37	- used by "POWER"
42	P _{MS} - power required at minimum ratio of power to velocity (hp)
43	P/V _f - the minimum calculated ratio of power to velocity
44	V _B - the upper bound velocity selected for the iteration (ft/sec)
45	VMR - the velocity at the minimum ratio of power to velocity (ft/sec)
46	V _{INC} - the velocity increment selected (ft/sec)

7. Program Listings

91+LBL "YMR"	36 1.6889
92 SF 93	37 /
03 *PSHP?*	38 /
94 PROMPT	39 RCL 43
95 STO 41	48 X>Y?
06 *Y-START?*	41 GTO 92
97 PROMPT	42 GTO 03
98 STO 45	43+LBL 02
99 1.68889	44 RCL Y
10 *	45 STO 43
11 STO 20	46 RCL 20
12 XEQ "DA"	47 STO 45
13 STO 42	48 RCL 37
14 RCL 41	49 STO 42
15 +	5 0+ LBL 93
16 RCL 45	51 RCL 44
17 /	52 RCL 20
18 STO 43	53 X<=Y?
19 *INCR?*	54 GTO 01
28 PROMPT	55 CF 93
21 1.6889	56 TONE 5
22 *	57 RCL 45
23 STO 46	58 1.6889
24 *Y-STOP?*	59 /
25 PROMPT	60 FIX 0
26 1.6889	61 "VMR="
27 *	62 ARCL X
28 STO 44	63 AVIEN
29+LBL 01	64 STOP
30 RCL 46	65 RCL 42
31 ST+ 20	66 " P< YMR >=
32 XEQ "PI"	67 ARCL X
33 RCL 41	68 AVIEN
34 +	69 STOP
35 RCL 29	70 EHD
AA MAM PA	

APPENDIX F

EVALUATION OF ANALYTICAL SOLUTIONS

1. This appendix contains comparisons of predicted performance data from an aircraft operator's manual with analytical results obtained by the use of computational programs developed in this study. The UH-60A helicopter (Blackhawk) was selected to conduct this comparison. Performance data for the UH-60A was taken from charts in Chapter 7 of TM 55-1520-237-10 (Operator's Manual). Performance data for the T700-GE 700 engine was taken from [Ref. 19]. Analytical calculations were made based upon the standard sea level performance characteristics of the T700-GE 700 engine (Appendix B) and the following design data for the UH-60A:

Main Rotor	Tail Rotor	Aircraft
C = 1.75 ft	C = 0.81 ft	L <tail> = 31.50 ft</tail>
R = 26.8 ft	R = 5.50 ft	W <gross> = 20,250 lbs</gross>
b = 4	b = 4	F.P.A.(FF) = 25.7
CdO = 0.008	CdO = 0.008	Vmax = 156 kts

RV = 27.2 rad/sec RV = 125 rad/sec

Program "POWER" was used to compute total power requirements (P_{T}) for the aircraft and the Helicopter Power Computation Package was used to verify the calculations. Calculation of fuel flow rates, maximum endurance velocity,

maximum range velocity, and fuel weight were all made on the HP-41C and verified using program "FUELFLO" and the Helicopter Computation Package on the IBM 3033 Computer.

2. Initially it was necessary to convert the percent torque readings from the charts in the Operator's Manual to Engine Shaft Horsepower (ESHP). The method used was as follows:

From [Ref. 23]:

Maximum continuous	<u>3</u>	Output Shaft	Output Torque		
Power at:	SHP	<u>RPM</u>	<u>(ft lb)</u>		
Stnd Sea Level	1310	20,000	344		

Solve for the torque conversion factor:

Torque (ft 1b) =
$$\frac{SHP \cdot 550(ft-1b/sec)(1/hp) \cdot 60}{20,000 \text{ rev/min}(2\pi \text{ rad/sec})}$$

= .263 SHP

Then from TM 55-1520-237-10 Fig 7-4 at Standard Sea Level conditions:

Maximum Continuous Torque Available = 88%

Therefore 100% Torque (the transmission limit) for two engines is:

2(344)/.88 = 792 ft-lb

or

792/.263 = 2973 ESHP

This value of 2973 ESHP is a constant limit for the transmission and was used to convert chart readings of

percent torque available to engine shaft horsepower for comparison with analytical results.

- 3. Comparisons.
 - a. ESHP and fuel flow rates: Table XI
 - b. Maximum endurance and maximum range velocities:
 Table XII
 - c. Mission profile fuel weight: Table XIII

TABLE XI

Analytical vs. Actual ESHP and Fuel Flow Rates

Standard Sea Level Conditions

	Analytical	Operator's <u>Manual</u>	% Error
Hover OGE ESHP W _f (lb/hr)	2399 1218	2676 1263	10 4
50 knots ESHP W _f (lb/hr)	1413 829	1635 895	14 7
100 knots ESHP W _f (lb/hr)	1276 775	1487 845	14 8
130 knots ESHP W _f (lb/hr)	1593 900	1903 975	16 8
4000 ft and 95 F	•		
Hover OGE ESHP W _f (lb/hr)	2575 1259	3122* 1400*	18 10
50 knots ESHP W _f (lb/hr)	1551 854	1932 970	20 12
100 knots ESHP W _f (lb/hr)	1245 733	1605 850	22 14
130 knots ESHP W _f (1b/hr)	1452 815	2021 1010	28 19

^{*}Approximate; exceeds maximum continuous power available.

TABLE XII

Analytical vs. Actual Max Endurance and Range Velocities

Standard Sea Level Conditions

	Analytical	Operator's <u>Manual</u>	% Error
Maximum Endurance Velocity (kts)	81	80	1
Maximum Range Velocity (kts)	140	142	1
4000 ft and 95 F			
Maximum Endurance Velocity (kts)	90	88	2
Maximum Range Velocity (kts)	149	129*	16

^{*}Exceeds maximum continuous power available.

TABLE XIII

Analytical vs. Actual Mission Fuel Weight

Conditions

PA = 4000 ft Cruise Velocity = 110 kts

Temp = 95 F Max Endurance Velocity:

Range = 275 nm = 88 kts (actual)

= 90 kts (analytical)

Normal Rated Power (2 engines):

= 2620 ESHP

Mission Fuel Weight Profile Equation

Fuel Weight = .05W_f<NRP> + W_f<cruise>*Range/V<cruise>
+ .25W_f<V<end>> + .05W_f<NRP>

Results

Operator's

Manual

% Error

Fuel	Weigh	nt (lbs)		2184		2343		7
Note:	Fuel	capacity	for the	UH-60A	is 2345	lbs.	This	
limited	l the	cruise ve	elocity	which	could be	used	to 110	
knots f	or th	is compar	ison.					

Analytical

INITIAL DISTRIBUTION LIST

		No. Copies
1.	Defense Technical Information Center Cameron Station Alexandria, Virginia 22314	2
2.	Library, Code 0142 Naval Postgraduate School Monterey, CA 93940	2
3.	Department Chairman, Code 67 Department of Aeronautics Naval Postgraduate School Monterey, CA 93940	1
4.	Professor Donald M. Layton, Code 67-Ln Department of Aeronautics Naval Postgraduate School Monterey, CA 93940	5
5.	CPT Timothy J. Casey 508 East 12th Street Oak Grove, MO 64075	1
6.	CPT James E. Young U.S. Army Aviation Safety Center Fort Rucker, AL 36362	1
7.	CPT Stephen G. Kee 1041 Edgefield Road	1

END

FILMED

F

10-83